WORKBOOK OF ATMOSPHERIC DISPERSION ESTIMATES

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Air Resources Field Research Office, Environmental Science Services Administration

U. S. DEPARTMENT OF HEALTH, EDUCATION, AND WELFARE Public Health Service Environmental Health Service National Air Pollution. Control Administration Cincinnati, Ohio Revised 1970 The ENVIRONMENTAL HIALTH SERIIDS of reports was estabilished to proport the results of esticities and angineering studies of marks environment: The community whether urban, assimute, or rural, where ha lives, works, and plays; the sir, in a way that preserve these neutran transcences. This SERIES of neuronsciences probasional users a control score of information on the intramment reason't activity produced users a control score of information on the intramment reason't activity in the server the server of the server. This SERIES of exposure that the probasional users a control score of information on the intramment reason't activity in the server of the server induction of the public states movings and the server of the server interscent server in the public states movings and the server of the server interscent server of the public states movings and the server of the server interscent server of the server interscent server of the public states movings and the server of the se

> AP — Air Pollution RH — Radiological Health

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PREFACE

This workhook presents some computational tachaiques currently used by scientism working with introspheric disposition problems. Because the basis working equition working with introspheric disposition problems. Because the basis working equiand judgment; such conductations are illustrated by 26 by requires special rules workhook is interacted as an aid to meteorologists and all publisms is centralise who are regulated to selfantise atmospheric concentrations of confurnitants from various types disposition estimates and the special spectra of the special spectra of the disposition estimates all of the numerous complications that are in making basis selfmeter of disposition cannot be as easily realwork. Awareness of the possible complexto realies when the services of a protocominal at publiciton meteophysical are seen one-

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ABSTRACT

This workbock presents methods of practical application of the hinomed toom timous plume dispusion model to estimate concentinations at in pollutants. Estimates of dispersion are those of Pasquill as restated by Oilford. Emplaneis in othe estimation of concentrations from continuous sources for simpling time up (a 1 hane. Some of the topics discussed are determination of effective height of emission, estamicion concentrations estimates to longer semiging intervals, invession brack-up immigation concentrations estimates to longer semiging intervals, invession brack-up immigation concentrations estimates to longer semiger piece. Some graphical acids to computation are included.

During recent years methods of estimating atmopheric dispersion have undergene considerable revision, primarily due to results of experimental measurements. In most diageneits merces the relevant atmospheric layer is that nearest the ground, wavying in tikiniess from several hundred to a few thousand meters. Variations in both years, and the several several several several velocity and greatest in the layer in contact with the autonome, inclusions from duced by huoyancy toress in the atmosphere is closely related to the vertices temperature structure. When temperature decreases with beight at a rate higher than 0.4^{-7} per 1000 f (1°C per 100 meters), the atmosphere is in unstable equilibrium and vertical metions are enhanced. When temperature decreases at a lower rate or increases with height (unversion), vertical motions are damped or reduced. Examples of typical versions are damped or reduced. Examples of typical versions in temperature and wind agood with height for daytime and nighttime conditions are illustrated in Fizure 1.1.

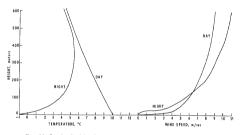


Figure 1-1. Examples of variation of temperature and wind speed with height (after Smith, 1963).

The termsfor of momentum upwerd or downword in the atcosophere is also related to stability: when the throughness is also related to stability: "definition," due to be a stable of the stability of the certain star index (nearly in the lowest have with high's than at high's (nearly in the lowest have counting the wind speed to increase more alony with high's than at high's (nearly in the lowest have counting the wind speed to increase more alony with high's than at high's (nearly in the lowest have the ground engineering the lowest have turbulence, which affects hout the dispersion of (wind into or wind with highly). Examples of these former 1.2. As wind speed increases, the effluent from a continuous source is introduced into a greater volume of air per unit time interval. In addition to this dilution by wind speed, the spreading of the material (normal to the mean direction of transport) by turbulence is a major factor in the dispersion process.

The procedures presented here to estimate atmospheric disposition are applicable when mean wind speed and direction can be determined, but measviments of turbulence, such as the standard deviation of wind direction fluctuations, are not available. If such measurements are at hand, techniques such as those outlined by Pasquill (1961) are likely to give more accurate results. The diffusion parameters presented hare are not applicable to groundiese (to to-level reliases (from the array factor to about 20 maters), although they are commonly applied at 30 maters), although they are commonly applied at throughout the diffusing layer, and no transluon throughout the diffusing layer, and no transluon throughout the diffusing layer, and the same diffusion of the same mean values for wind diffuction of the same same values to wind diffusion with height in the mixing layer are taken into account. This usually is not a problem in matrix lo unstable (e.g., daydime) stratistics, hat can ensue table conditions. discussion diffusion diffusion of the same diffusion table conditions.

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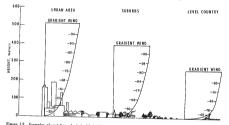


Figure 1-2. Examples of variation of wind with height over different size roughness elements (tigures are percentages of gradient wind); (from Davenport, 1963).

For a number of years estimates of concentrations were calculated either from the equations of Sutton (1932) with the atmospheric dispersion parameters C_{γ} , C_{α} , and n, or from the equations of Bosanquet (1936) with the dispersion parameters p and q.

Hay and Pasquill (1957) have presented experimental evidence that the vertical distribution of spreading particles from an elevated point is related to the standard deviation of the wind elevation angle, vs. at the point of release. Cramer (1957) derived a diffusion equation incorporating standard deviations of Gaussian distributions; e. for the distribution of material in the plume across wind in the horizontal, and a, for the vertical distribution of material in the plume. (See Annendix 2 for pronerties of Gaussian distributions.) These statistics were related to the standard deviations of azimuth angle, and elevation angle, and calculated from wind measurements made with a hi-directional wind vane (bivane). Values for diffusion parameters based on field diffusion tests were suggested by Cramer, et al. (1958) (and also in Cramer 1959a and 1959b). Hay and Pasquill (1959) also presented a method for deriving the spread of pollut-ants from records of wind fluctuation. Pasquill (1961) has further proposed a method for estimating diffusion when such detailed wind data are not available. This method expresses the height and angular spread of a diffusing plume in terms of more commonly observed weather parameters. Suggested curves of height and angular spread as a function of distance downwind were given for several "stability" classes. Gifford (1961) converted Pasquill's values of angular spread and height into standard deviations of plume concentration distrihution, or and op. Pasquill's method, with Gifford's conversion incorporated, is used in this workbook (see Chapter 3) for diffusion estimates.

Advantages of this system are that (1) only two dispersion parameters are required and (2) results of most diffusion experiments are now being ported in terms of the standard deviations of plume spread. More field dispersion experiments are being conducted and will be conducted under conditions conducted and will be conducted under conditions conducted and will be conducted under conditions for the standard deviation of the standard protein the standard deviation of the standard deviation bility. If the dispersion parameters from a specific constitution of the standard deviation of than those suggested in this workbook, the parametor values can be used with the equations given here.

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is chapter outlines the basic procedures to id in making dispersion estimates as sugby Pasquill (1961) and modified by Gifford

DINATE SYSTEM

the system considered here the origin is at $1 | \operatorname{svel} a$ to beneat the point of emission, ve x-sxie extending horizontally in the directly the mean wind. The y-axis is in the hori-plane parpendicular to the x-axis, and the extends vertically. The plane travels along illel to the x-axis. Figure 3-1 illustratos the late system.

SION EQUATIONS

concentration, x, of gas or acrosols (partiss than about 20 microns diameter) at x,y,z continuous source with an effective emission

H, is given by equation 3.1. The notation o depict this concentration is χ (x,y,z;H). he height of the plume centerline when it become assantially level, and is the sum of the physical stack-height, h, and the hymor rise, ALT. The following assumptions are made: the phume spreads has a Gaussian distribution (see Appendix 2) in both the horizontal and vertice that the starbution in the horizontal and vertice that one distribtion is used to the inform emission rate of pollutants is \mathbf{G}_i and total reflection of the phume shores that the startes phume is the startes (see Section 2).

$$\begin{split} \chi\left(\mathbf{x},\mathbf{y},\mathbf{y},\mathbf{H}\right) &= \frac{\mathbf{Q}}{2\pi\sigma_{1}\sigma_{1}\sigma_{1}}\exp\left[-\frac{1}{2}\left(\frac{\mathbf{y}}{\sigma_{2}}\right)^{2}\right] \\ \left\{\exp\left[-\frac{1}{2}\left(\frac{\mathbf{z}\cdot\mathbf{H}}{\sigma_{n}}\right)^{2}\right] + \exp\left[-\frac{1}{2}\right] \\ \left(\frac{\mathbf{z}\cdot\mathbf{H}}{\sigma_{n}}\right)^{2}\right]\right\} \end{split} \tag{3.1}$$

*Note: exp -a/b == e^{-a/b} where e is the base of natural legarithms and is approximately equal to 2.7183.

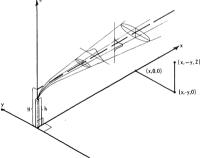


Figure 3-1. Coordinate system showing Gaussian distributions in the horizontal and vertical.

tes

Any consistent set of units may be used. The most common is:

χ (g m⁻¹) or, for radioactivity (curies m⁻¹) Q (g sec⁻¹) or (curies sec⁻¹) u (m sec⁻¹) σ₁, σ_n H.x.y. and z (m)

This equation is the same as equation (3.33) p. 393 of Sutton (1953) when s's are substituted for Suttor's parameters through equations like (3.27) p. 295. For evaluations of the exponentials found in Eq. (3.1) and those that follow, see Appendix 3 χ is a mean over the same time interval as the time interval for which the s's and u are expresentative. The values of both s, and e, are evaluated in terms of the downwind distance, χ .

Eq. (3.1) is valid where diffusion in the direction of the plume travel can be neglected, that is, no diffusion in the x direction.

This may be assumed if the release is continuous or if the duration of release is equal to or greater than the travel time (x/u) from the source to the location of interest.

For concentrations calculated at ground level, i.e., $z=0, \mbox{ (see problem 3) the equation simplifies to: }$

$$\chi (\mathbf{x}, \mathbf{y}, \mathbf{0}; \mathbf{H}) = \frac{\mathbf{Q}}{\pi \sigma_r \sigma_x \mathbf{u}} \exp \left[-\frac{1}{2} \left(\frac{\mathbf{y}}{\sigma_r} \right)^{2} \right]$$

$$\exp \left[-\frac{1}{2} \left(\frac{\mathbf{H}}{\sigma_r} \right)^{2} \right] \qquad (3.2)$$

Where the concentration is to be calculated along the centerline of the plume (y - 0), (see problem 2) further simplification results:

$$\chi$$
 (x,0,0;H) = $\frac{Q}{\pi \sigma_{\gamma} \sigma_{t} u} \exp \left[-\frac{1}{2} \left(\frac{H}{\sigma_{c}}\right)^{2}\right]$ (3.3)

For a ground-level source with no effective plume rise (H - 0), (see problem 1);

$$\chi (x,0,0;0) = -\frac{Q}{\pi \sigma_y \sigma_z u}$$

(3.4)

EFFECTS OF STABILITY

The values of s_{y} and s_{y} vary with the turbulest structure of the atmosphere, height above the autiface, surface roughness, sampling time over which the concentration is to be estimated, wind speed, and distance from the source. For the parameter values given here, the sampling time is assured to low the surface to be multively openophere, and the surface to be multively openophere, and wind speed are considered in the atmosphere and wind speed are considered in the atmosphere and wind smtad, and the effect of distance from the source is considered in the graphs determining the partometer encoder of the graph determining the partometer determining that the source of the source of

Table 3-1 KEY TO STABILITY CATEGORIES

Surface Wind Speed (at 10 m), n sec-1		Day Incoming Solar Radiation			Night	
					Thinly Overcast	=3/8
		Strong Mo	Moderate	ocierate Slight	ar ≌4/8 Low Cloud	Cloud
<	2	Α	A A-B	В		
	2-3	A-B	В	C	E.	F
	3-5	В	B-C	С	D	Е
	5-6	С	C-D	D	D	D
>	6	C	D	D	D	D

The nostral class, D, should be assumed for overcost conditions during day or night.

"Strong" incoming solar radiation corresponds to a solar altitude greater than 60° with clear skies; "slight" insolation corresponds to a solar altitudo from 15° to 35° with clear skies. Table 170, Solar Altitude and Azimuth, in the Smithsonian Meteorological Tables (List, 1951) can be used in determining the solar altitude. Cloudiness will decrease incoming solar radiation and should be considered along with solar altitude in determining solar radiation. Incoming radiation that would be strong with clear skies can be expected to he reduced to moderate with broken (% to % cloud caver) middle clouds and to slight with broken low clouds. An objective system of classifying stability from hourly meteorological observations based on the above method has been suggested (Turner, 1961).

ATMOSPHERIC DISPERSION ESTIMATES

Some proliminary results of a dispersion experiment in St. Louis (Pooler, 1965) showed that the dispersion over the city during the daytime behaved somewhat like types B and C; for one night experiment a_i varied with distance between types D and E.

ESTIMATION OF VERTICAL AND HORIZONTAL DISPERSION

Having determined the stability class from Table 3-1, one can evaluate the estimates of a, and a, as a function of downwind distance from the source, x, using Figures 3-2 and 3-3. These values of a, and a, are representative for a sampling time of about 10 minutes. For estimation of concentrations for longer time periods see Chapter 5. Figures 3-2 and 3-3 apply strictly only to open level country and probably underestimate the plume dispersion notential from low-level sources in built-up areas. Although the vertical spread may be less than the values for class F with very light winds on a clear night, quantitative estimates of concentrations are nearly impossible for this condition. With very light winds on a clear night for ground-level sources free of topographic influences, frequent shifts in wind direction usually occur which serve to spread the plume horizontally. For elevated sources under these extremely stable situations, significant concentrations usually do not reach ground level until the stability changes.

A stable layer existing above an unstable layer will have the effect of restricting the vertical diffusion. The dispersion computation can be modified for this situation by considering the height of the base of the stable layer. L. At a height 2.15 g. above the plume centerline the concentration is onetenth the plume centerline concentration at the same distance. When one-tenth the plume centerline concentration extends to the stable layer, at height L, it is reasonable to assume that the distribution starts being affected by the "lid." The following method is suggested to take care of this situation. Allow e, to increase with distance to a value of L/2.15 or 0.47 L. At this distance x., the plume is assumed to have a Gaussian distribution in the vertical. Assume that by the time the plume travels twice this far, 2 x1, the plume has become uniformly distributed between the earth's surface and the height L, i.e., concentration does not vary with height (see Figure 3-4). For the distances greater than 2 xr., the concentration for any height between the ground and L can be calculated from;

$$\chi (\mathbf{x}, \mathbf{y}, \mathbf{z}; \mathbf{H}) = \frac{\mathbf{Q}}{\sqrt{2\pi} \sigma_y \mathbf{L} \mathbf{u}} \exp \left[-\frac{1}{2} \left(\frac{\mathbf{y}}{\sigma_y} \right)^3 \right]$$

for any \mathbf{z} from 0 to \mathbf{L} (3.5)

for $x \ge 2 x_L$; x_L is where $\sigma_b = 0.47 L$

(see problem 6). Note that Eq. (3.5) assumes normal or Gaussian distribution of the plume only in the horizontal plane. The same result can be obtained from the following equation where $\sigma_{\rm rL}$ is an effective dispersion parameter because $\sqrt{2\pi}$ I. == 2.066 L and 0.8 π L = 2.61 L.

$$\chi$$
 (x,y,z;H) = $\frac{Q}{\pi \sigma_s \sigma_{sl}, u} \left[\exp \left[-\frac{1}{2} \left(\frac{y}{\sigma_r} \right)^z \right] \right]$

(3.6)

for any z from 0 to L for x >2_{st.}; x_t is where $\sigma_{\rm a} = 0.47$ L The value of $\sigma_{\rm st.} = 0.8$ L

EVALUATION OF WIND SPEED

For the wind speed, u, a mean through the vertical actent of the plume should be used. This would be from the height $H - 2 \ a_{\rm s}$ through $H + 2 \ a_{\rm s}$ of course if $2 \ a_{\rm s}$ is greater than H then the wind can be averaged from the ground to $H + 2 \ a_{\rm s}$. However, the "surface wind" value may be all that how the three of low-level emissions, especially under stable conditions.

PLOTS OF CONCENTRATIONS AGAINST DISTANCE

To gain maximum insight into a diffusion problem it is often desimble to pict centarine concentrations against distance downwind. A convenient procedure is to detarmine the ground-level centerline concentrations for a number of downwind distances and pict lines values and tog-log graph paper. Contrations for intermediate downwind distances (see problem 6).

ACCURACY OF ESTIMATES

Because of a multitude of scientific and technical limitations the diffusion computation method presented in this manual may provide best estimates but not infallible predictions. In the unstable and stable cases, severalfold errors in estimate of ex can occur for the longer travel distances. In some cases the ag may be expected to be correct within a factor of 2, however. These are: (1) all stabilities for distance of travel out to a few hundred meters; (2) neutral to moderately unstable conditions for distances out to a few kilometers; and (3) unstable conditions in the lower 1000 meters of the atmosphere with a marked inversion above for distances out to 10 km or more. Uncertainties in the estimates of σ_x are in general less than those of σ_x . The ground-level centerline concentrations for these

Estimates

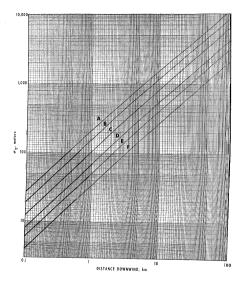


Figure 3-2. Horizontal dispersion coefficient as a function of downwind distance from the source.

ATMOSPHERIC DISPERSION ESTIMATES

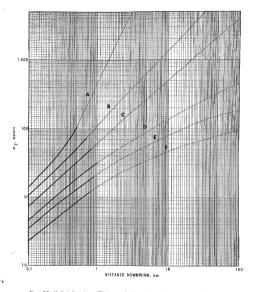


Figure 3-3. Vertical dispersion coefficient as a function of downwind distance from the source.

Estimates

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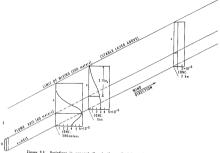


Figure 3-4. Variations in concentration in the vertical beneath a more stable laver.

three cases (where σ_i can be expected to be within a factor of 2) should be correct within a factor of 3, including errors in σ_i and u. The relative confidence in the σ^{i} s (in decreasing order) is indicated by the heavy lines and dashed lines in Figures 3-2 and 3-3.

Estimates of H, the effective height of the plume, may be in error because of uncertainties in the estimation of aH, the plume, Aiso, for problems that require estimates of course, Aiso, for problems the difficulty of determining the mean wind over a given time interval and consequently the location of the x-axis can cause considerable uncertainty.

GRAPHS FOR ESTIMATES OF DIFFUSION

To avoid regolitions computations, Figure 3.5 (A through P) gives relative pround-level concentrations times wind speed ($\chi = 0/2$ gainst downwind distance for various effective heights of emission and image to the vertical mixing for each stations was made from Eq. (3.3), (3.4), and (3.5). Estimates of actual concentrations may be determined by multiplying excluste values by Q/ω .

PLOTTING GROUND-LEVEL CONCENTRATION ISOPLETHS

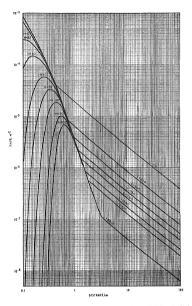
Often one wishes to determine the locations where concentrations equal or exceed a given maynitude. First, the axial position of the plume must be determined by the mean wind direction. For plotting isopleths of ground-level concentrations, the relationship between ground-level encountertutions can be used:

$$\frac{\chi (\mathbf{x}, \mathbf{y}, \mathbf{0}; \mathbf{H})}{\chi (\mathbf{x}, \mathbf{0}, \mathbf{0}; \mathbf{H})} \rightarrow \exp \left[-\frac{1}{2} \left(\frac{\mathbf{y}}{\sigma_{\mathbf{y}}}\right)^{2}\right]$$
 (3.7)

The y coordinate of a particular isopleth from the x-axis can be determined at each downwind distance, x. Suppose that one wishes to know the off-axis distance to the 10^{-3} g m⁻³ isopleth at au x of 600 m, under stability type B, where the groundlevel centerline concentration at this distance is 2.9 x 10^{-3} g m⁻³.

$$\frac{\exp \left[-\frac{1}{2}\left(\frac{y}{\sigma_{r}}\right)^{2}\right] - \frac{\chi(x,y,0;H)}{\chi(x,0,0;H)}}{\frac{10^{-5}}{2.9 \times 10^{-1}} = 0.345}$$

ATMOSPHERIC DISPERSION ESTIMATES





Estimates

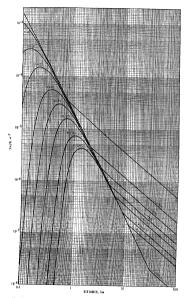


Figure 3-58. xu/Q with distance for various heights of emission (H) and limits to vertical dispersion (L), B stability.

ATMOSPHERIC DISPERSION ESTIMATES

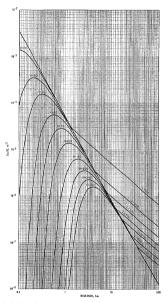


Figure 3-5C. xu/Q with distance for various heights of emission (H) and limits to vertical dispersion (L), C stability.

Estimates

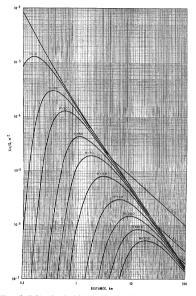


Figure 3-5D. xu/Q with distance for various heights of emission (H) and limits to vertical dispersion (L), D stability,

ATMOSPHERIC DISPERSION ESTIMATES

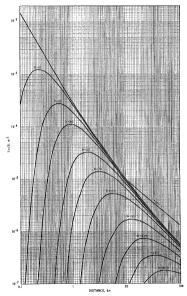


Figure 3-5E. xu/Q with distance for various heights of emission (H) and limits to vertical dispersion (L), E stability.

Estimates

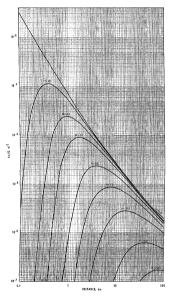


Figure 3-5F. xu/Q with distance for various heights of emission (H) and limits to vertical dispersion (L), F stability.

ATMOSPHERIC DISPERSION ESTIMATES

From Table A-1 (Appendix 3) when exp

$$\left[-\frac{1}{2}\left(\frac{y}{\sigma_{f}}\right)^{2}\right] = 0.345, y/\sigma_{f} = 1.46$$

From Figure 3-2, for stability B and x = 600 m, σ_r = 92. Therefore y = (1.46) (92) = 134 meters. This is the distance of the 10^{-2} isopleth from the x-axis at a downwind distance of 660 meters.

This can also be determined from:

$$y = \left\{ 2 \ln^{\alpha} \left[\frac{\chi (x,0,0;H)}{\chi (x,y,0;H)} \right] \right\}^{\frac{1}{2} \sigma_{\gamma}} \quad (3.8)$$

The position corresponding to the downwind distance and of-axis distance can then be plotted. After a roumber of points have been plotted, then a roumber of points have been plotted, then isophetical of $_{\rm AU}$ (P or vertices stabilities for sources at H ~ 0 and H ~ 100 meters. For example, to locate the 10⁻⁴ g m⁻¹ isophetic resulting from a locate the 10⁻⁴ g m⁻¹ isophetic resulting from a conditions with wind gade 2 m sec. one must first distribution the isometers be $_{\rm AU}$ (P $_{\rm AU}$ (P $_{\rm AU}$) the is the quantity graphed in Figure - one must first distribution the corresponding value of $_{\rm AU}$ (P $_{\rm AU}$) provide to a 'solorability of the route of $_{\rm AU}$ (P $_{\rm AU}$) seconds to a 'solorability of the route of $_{\rm AU}$ (P $_{\rm AU}$) seconds to a 'solorability with a value of 10⁻⁵ g m⁻¹.

AREAS WITHIN ISOPLETHS

Figure 3-8 gives aross within isopleths of groundlevel concentration in terms of $\chi u/Q$ for a groundlevel source for various stability categories (Gifford, 1962; Hilameier and Gifford, 1962). For the example just given, the area of the 10^{-3} g m⁻³ isopleth $(10^{-1} m^{-3} \chi u/Q)$ sopleth b) is about 5-10⁻⁶ meters.

CALCULATION OF MAXIMUM GROUND-LEVEL CONCENTRATIONS

Figure 3-9 gives the distance to the point of maximum consentation, u_{max} and B matrix marchimatching and B_{max} and B_{max} and B_{max} and effective height of emission and stability class (Marcin, 1065). This figure was approved from the stability of the stability of the stability of the emission height and stability and multiplying the emission height and stability and multiplying the remaining the stability of the stability of the stability discrements with height and the increases with

""In" denotes natural logarithms, i.e., to the base e.

Estimates

height, the product $u_{\sigma_{j}} \sim will not change appreci$ ably. The greater the effective height, the morelikely it is that the stability may not be the samefrom the ground to this height. With the longertravel distances such as the points of maximumconcentrations for stable conditions (Types E orF), the stability may change before the plumetravels the entire distance.

REVIEW OF ASSUMPTIONS

The preceding has been based on these assumptions, which should be clearly understood:

(i) Continuous emission from the source or emission times equal to or greater than travel times to the downwind position under consideration, so that diffusion in the direction of transport may be neglected.

(ii) The material diffused is a stable gas or aerosol (less than 20 microns diameter) which remains suspended in the sir over long periods of time,

(iii) The equation of continuity:

$$Q = \int_{0}^{+\infty} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} u \, dy \, dz \qquad (3.9)$$

is fulfilled, i.e., none of the material emitted is removed from the plume as it moves downwind and there is complete reflection at the ground.

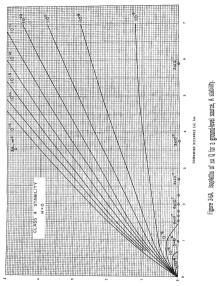
(iv) The mean wind direction specifies the x-axis, and a mean wind speed representative of the diffusing layer is chosen.

(v) Except where specifically mentioned, the plume constituents are distributed normally in both the cross-wind and vertical directions.

(vi) The σ's given in Figures 3-2 and 3-3 represent time periods of about 10 minutes.

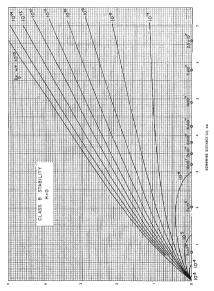
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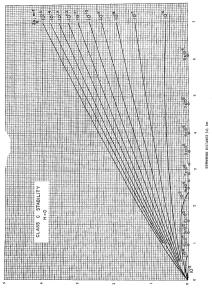


CSO22MIND DI2LVNCE {*)' P*

ATMOSPHERIC DISPERSION ESTIMATES



CROSSIMING DISTANCE (4)' Fm



CEO22MIND DI21VNCE (^k)' F

ATMOSPHERIC DISPERSION ESTIMATES

Figure 3-6C. Isopleths of $\chi u'Q$ for a ground-level source, C stability

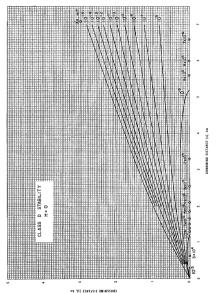
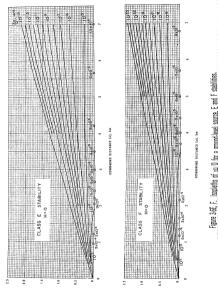


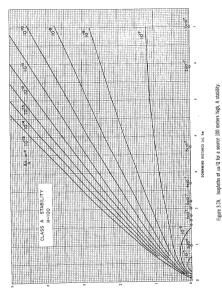
Figure 3-6D. Isopleths of xu/Q for a ground-level source, D sta

Estimates



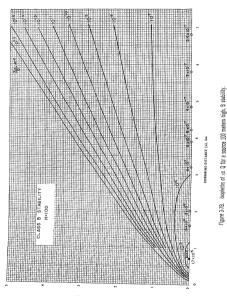
CROSSWING DISTANCE [y]. X=

ATMOSPHERIC DISPERSION ESTIMATES



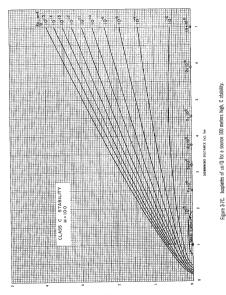
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Estimates



CROSSWIND DISTANCE [V], Km

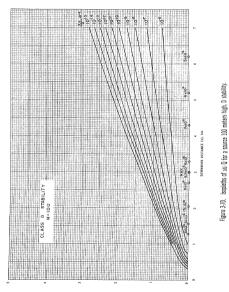
ATMOSPHERIC DISPERSION ESTIMATES



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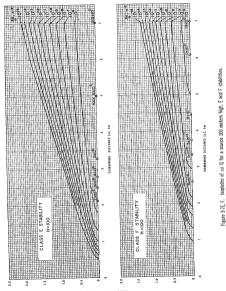
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339-905 0 - 89 - 3



USERVICE (A): Fm

ATMOSPHERIC DISPERSION ESTIMATES



CROSSWIND DISTANCE (*)' Km

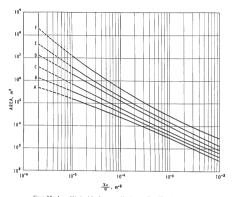


Figure 3-8. Area within isopleths for a ground-level source (from Hilsmeier and Gifford).

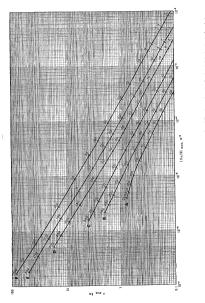
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ATMOSPHERIC DISPERSION ESTIMATES





ates

GENERAL CONSIDERATIONS

In most problems one must estimate the effective stack height, H, at which the plume becomes essentially level. Rarely will this height correspond to the physical height of the stack, h. If the nume is cought in the turbulent wake of the stack or of buildings in the vicinity of the stack, the offluent will be mixed rapidly downward toward the ground (aerodynamic downwash). If the plume is emitted free of these turbulent zones, a number of emission factors and meteorological factors influence the rise of the plume. The emission factors are: velocity of the effluent at the top of the stack, v.; temperature of the effluent at the top of the stack. T .: and diameter of the stack opening, d. The meteorological factors influencing plume rise are wind speed, u: temperature of the air. T.: shear of the wind speed with height, du/dz; and atmospheric stability. No theory on plume rise takes into account all of these variables; even if such a theory were available, measurements of all of the parameters would seldom be available. Most of the equations that have been formulated for computing the effective height of emission are semi-empirical. For a recent review of equations for effective height of emission see Moses, Strom, and Carson (1964).

Morea and Strom (1981), having compared actaul and calculated plures heights by means of air plunes rise equations, report "There is no one low formulas of Davidson-Byrom (1996), Halland (1985), Boanquet-Carcoy-Inition (1990), and Boanquet (1997) in give generally assisted analysis of the start of the start of the start of the database of the start of the start of the start database of the start of the start of the start from a nize of less than 0.5 meter dimeter than 40 meters and particulations in the start of th

The equation of Holland was developed with experimental data from larger sources than those of Moses and Strom (stack diameters from 1.7 to 204°C); Holland's equation is used in the solution of the problems given in this workhook. We beight the environment of the solution of the beight of the solution is a solution of the beight of the solution of the solution of the beight of solution of the solution of the solution of the "solution" theorem of the solution of the beight of solution of the solution of the solution of the beight "solution" theorem of the solution of t

Holland's equation is:

$$\Delta H = \frac{v_s d}{u} (1.5 + 2.68 \times 10^{-5} p \frac{T_s - T_s}{T_s} d) (4.1)$$

where;

AH - the rise of the plume above the stack, m

Effective Height

v. - stack gas exit velocity, m sec-1

d - the inside stack diameter, m

u - wind speed, m sec-1

n - atmospheric pressure, mh

T. - stack gas temperature, °K

T. - air temperature, °K

and 2.68 x $10^{-_{\rm 0}}$ is a constant having units of mb^-_1 m^-_1.

Holiand (1953) suggests that a value between 1.1 and 1.2 times the AH from the equation should be used for unstable conditions; a value between 0.8 and 0.9 times the AH from the equation should be used for stable conditions.

Since the plume rise from a stack occurs over some distance downwind, Eq. (4.1) should not be applied within the first few hundred meters of the stack.

EFFECTIVE HEIGHT OF EMISSION AND MAXIMUM CONCENTRATION

If the effective heights of emission were the same under all atmospheric conditions, the highest ground-level concentrations from a given source would occur with the lightest winds. Generally, however, emission conditions are such that the effective stack height is an inverse function of wind speed as indicated in Eq. (4.1). The maximum cround-level concentration occurs at some intermediate wind sneed, at which a balance is reached between the dilution due to wind speed and the effect of height of emission. This critical wind speed will vary with stability. In order to determine the critical wind speed, the effective stack height as a function of wind speed should first be determined. The maximum concentration for each wind speed and stability can then he calculated from Figure 3-9 as a function of effective height of emission and stability. When the maximum concentration as a function of wind speed is plotted on log-log graph paper, curves can be drawn for each stability class; the critical wind speed corresponds to the point of highest maximum concentration on the curve (see problem 14).

ESTIMATES OF REQUIRED STACK HEIGHTS

Estimates of the stack height required to produce concentrations below a given value may be made through the use of Figure 3-9 by obtaining solutions for various wind speeds. Use of this figure considers maximum concentrations at any distance from the source.

In some situations high concentrations upon the property of the emitter are of little concern, but

maximum concentrations beyond the property line are of the utmost importance. For first approximations it can be assumed that the maximum concentration occurs where $\sqrt{2} \sigma_{u} \rightarrow \mathbf{H}$ and that at this distance the σ 's are related to the maximum concontration by:

$$\sigma_{\gamma} \sigma_{\chi} \simeq \frac{Q}{\pi u \mathbf{c} \chi_{max}} \simeq \frac{0.117 Q}{u \chi_{max}}$$
(4.2)

Knowing the source strength, Q. and the concentration not to be exceeded your one can determine the necessary a. a. for a given wind speed. Figure 4-1 shows e. e. as a function of distance for the various stability classes. The value of a, a, and a design distance, x4 (the distance beyond which x is less than some pre-determined value), will determine a point on this graph yielding a stability class or point between classes. The a, for this stability (or point between atabilities) can then be determined from Figure 3-3. The required effective stack height for this wind speed can then be approxi-mated by $H = \sqrt{2} \sigma_c$ (see problem 15). Since Eq. (4.2) is an approximation, the resulting height should be used with Eq. (3.3) to ensure that the maximum concentration is sufficiently low. If enough is known about the proposed source to allow use of an equation for effective height of emission, the relation between ΔH and u can be determined. The physical stack height required at the wind speed for which H was determined is H ---AH. The same procedure, starting with the determination of ev es, must be used with other wind speeds to determine the maximum required physical stack height (see problem 16).

EFFECT OF EVAPORATIVE COOLING

When effluent games are washed to absorb ontain constituents prior to crusission, the games are cooled and become saturated with water vaper. Upon robases of the games from the absorption tower, of ductowell or stack is Mely. This cooling causes condensation of water droplets in the gas stream. Upon robases of the gases from the stack, the water droplet a exponence, withdrawing the latent hat of waperization from the sit and cooling the plane. Upon stream of the Gover, 1999.

EFFECT OF AERODYNAMIC DOWNWASH

The influence of mechanical turbulence around a building or stack can significantly alter the effective stack height. This is especially true with high winds, when the beneficial effect of high stackgas velocity is at a minimum and the plume is emitted nearly horizontally. The region of disturbed flow surrounds an isolated huiding, generally to at least twice its height and extends downwind 5 to 10 times its height. Building the stack 2.5 times the height of the highest building adjacent to the stack usually overcomes the effects of building turbulence (Hawkins and Nonhebel, 1955). Ensuring that the exit velocity of the stack gas is more than 1.5 times the wind speed will usually prevent downwash in the wake of the stack. Most of the knowledge about the turbulent walces around stacks and buildings has been gained through wind tunnel studies (Sherlock and Lesher, 1954; Strom, 1955-1956; Strom, et al. 1957; and Halitsky, 1962). By use of models of building shapes and stacks, one may determine the wind speeds required to cause downwash for various wind directions. With a wind tunnel the meteorological variables most easily accounted for are wind speed and wind direction (hy rotation of the model within the tunnel). The emission factors that may be considered are the size and shape of the plant huilding: the shape, height, and diameter of the stack; the amount of emission; and the stackgas velocity.

Through wind tunnel studies, the critical wind speeds that will cause downwash from various directions can be determined for a given set of plant isotras. The average number of hours of downwash per years can then be calculated by dotermining the frequency of wind speeds gracing than the critical frequency of wind speeds gracing than the critical 1954) if climatological data representative of the sito are available.

Maximum downwash about a rectangular structure occurs when the direction of the wind is at an angle of 45 degrees from the major axis of the structure; minimum downwash occurs with wind flow parallel to the major axis of the structure (Sherback and Lesier, 1954).

Halitzky (1961, 1963) has shown that the effluent from flash openings on flat mode fragmently flows in a direction opposite to that of the free atmosphere' wind, owing to counter-flow along the roof in the turbulent wake above the building. In addition to the effect of aerodynamic downwash upon the release of air pollutants from stacks and building, one must lake consider the effects of aerodynamic downwash when exposing meteorological instruments near ou quon buildings.

Where the pollution is emitted from a vert or opening on a building and is immediately infinienced by the turbulent wake of the building, the pollution is rapidly distributed within this turbulent wake, non may seame hinormal distributions of concentrations at the source, with horizontal and tandard deviations are valided to the width and height of the building, for example, letting 4.3 σ_T equal the width of the building and 2.15 σ_T even

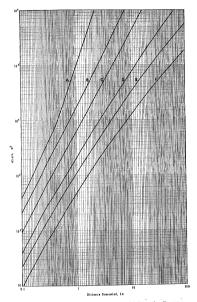


Figure 4-1. The product of $\sigma_{y\sigma_{0}}$ as a function of downwind distance from the source.

the height. Values other than 4.3 and 2.15 can be used. When these values are used 97% of the distribution is included within these limits. Virtual distances x_1 and x_2 on $be (and such that at <math>x_1$ $\sigma_1 \rightarrow \sigma_n$ and $at x_2$ m_p . These t's will differ with stability. Equations applicable to point sources can then be used, determining σ_1 as a function of $x + x_n$ and a_n as a function of $x + x_n$.

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CONCENTRATIONS IN AN INVERSION BREAK-UP FUMIGATION

A surface-based investion may be eliminated by ground audice when that surface is warmer thus ground audice when that surface is warmer thus ground is body warmed by solar radius of the surface surface and the surface surface and the in effects statistical pointaints prevent the suited werkfally when they are randout by the thermal define, and ground-belowed methods and interace. Surface and cliff (1964) and Herror (1964). Fourtions for estimating concentrations with these conditions for estimating concentrations with these conditions for estimating (1965). Fourdances of the surface of the surface and difficult and the surface of the difficult here (1965).

To estimate ground-level concentrations under inversion break-up furnigations, one assume that the plume was initially emitted into a stable layer. Tamefore, η_{e} and η_{e} characteristic of stable conditions must be selected for the particular distance of concern. An equation for the ground-level conemtration when the inversion has been eliminated in a builth h.is:

$$\begin{split} \chi_{\mathbf{p}} & (\mathbf{x}_{\mathbf{y}} 0; \mathbf{f}) \mapsto \mathbf{p} \\ \mathbf{q} & \left[\int_{-\infty}^{0} \frac{1}{\sqrt{2\pi}} \exp \left(-0.5 \, \mathbf{p}^{*} \right) \, \mathrm{d}\mathbf{p} \right] \\ \frac{\sqrt{2\pi} \sigma_{\mathbf{p}} u \, \mathbf{h}_{\mathbf{h}}}{\exp \left[-\frac{1}{2} \left(\frac{1}{\sqrt{p}} \right)^{*} \right]} & \text{(5.1)} \end{split}$$
where $\mathbf{p} = \frac{\mathbf{h}_{\mathbf{h}} - \mathbf{H}_{\mathbf{q}}}{\sigma_{\mathbf{q}}}$

and gay is discussed below.

Values for the integral in brackets can be found in most statistical tables. For example, see opse 273– 276, Burington (1963). This factor accounts for the portion of the plume that is mixed downward. If the inversion is elimitated up to the effective stack height, half of the plume is presumed to be mixed downward, the other half remaining in the stable at above. Eq. (63) can be approximated when the furnigation concentration is near its maximum by:

$$\chi_{\mathbf{r}} (\mathbf{x}, \mathbf{y}, 0; \mathbf{H}) = \frac{\mathbf{Q}}{\sqrt{2\pi} \mathbf{u} \sigma_{\mathbf{r}\mathbf{r}} \mathbf{h}_{\mathbf{i}}} \exp \left[-\frac{1}{2} \left(\frac{\mathbf{y}}{\sigma_{\mathbf{r}\mathbf{r}}}\right)^{*}\right]$$

(5.2)

$$h_t = H + 2 \sigma_s = h + \Delta H + 2 \sigma_s \qquad (5.3)$$

Special Topics

A difficulty is encountered in estimating a reasomable value for the horizontal dispersion since in mixing the stable plume through a vertical depth some additional horizontal spreading occurs (see problem 12). If this spreading is ignored and the g, for stable conditions used, the probable result would be estimated concentrations higher than actual concentrations. Or, using an approximation suggested by Bierly and Hewson (1962) that the edge of the plume spreads outward with an angle of 15°, the gree for the inversion break-un fumigation equals the oy for stable conditions plus one-eighth the effective height of emission. The origin of this concept can be seen in Figure 5-1 and the following equation, where the edge of the plume is the point. at which the concentration falls to 1/10 that at the centerline (at a distance of 2.15 g, from the plume center).

$$\sigma_{19} = \frac{2.15 \sigma_{y} \text{ (stable)} + \text{H tan } 15^{\circ}}{2.15}$$

= $\sigma_{e} \text{ (stable)} + \text{H/8}$ (5.4)

A Gaussian distribution in the horizontal is assumed.

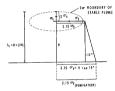


Figure 5-1. Diagram showing assumed height, h and or during fumigation, for use in equation (5.2).

Eq. (5.4) should not be applied next the stack, for if the investment has been diministed to a height antificient to include the enrice plume, the emission is taking place under unstable to catishe conditions. Therefore, the nearest downwind distance to be considered for an estimate of fungistion concentrations must be great enough, based on the time required to elimitate the inversion, that this portion of the plane was initially emitted into stable at. "This distance is $x \to u$, where u is flat ensure to the start of the start. This distance is $x \to u$, where u is flat ensure to the start of the start

wind in the stable layer and t_u is the time required to eliminate the inversion from h, the physical height of the stack to h, (Eq. 5.3).

t_s, is dependent upon both the strength of the inversion and the rate of heating at the surface. Pooler (1965) has derived an expression for estimating this time:

$$t_n = \frac{\rho_n c_p}{R} \frac{\delta \theta}{\delta z} (h_l - h) \left(\frac{h + h_l}{2}\right)$$
 (5.5)

- where t_{in} -- time required for the mixing layer to develop from the top of the stack to the top of the plume, sec
 - Pa ambient air density, g m-s
 - cp -- specific heat of air at constant pressure, cal g^{-1} °K^{-1}
 - R net rate of sensible heating of an air column by solar radiation, cal m⁻⁹ sec⁻¹
 - $\frac{\delta\Theta}{\delta_s}$ vertical potential temperature gradient, $^{\circ}K m^{-1} - \frac{\delta T}{\delta z} + \Gamma$ (the adiabatic lapse rate)
 - h_i -- height of base of the inversion sufficient to be above the plume, m
 - h physical height of the stack, m

Note that h_i —h is the thickness of the layer to be heated and $\left(\frac{h+h_i}{2}\right)$ is the average height of the layer. Although R depends on season, and cloud cover and varies continuously with time. Pooler has used a value of 67 cal m^{-s} sec⁻¹ as an average for formization.

Hewson (1945) also suggested a method of estimating the time required to eliminate an inversion to a height z by use of an equation of Taylor's (1915, p. 8):

$$t = \frac{z^{i}}{4 K}$$
 (5.6)

- where: t -= time required to eliminate the inversion to height z, sec
 - z -- height to which the inversion has been eliminated, m
 - K eddy diffusivity for heat, m² sec⁻¹

Rewriting to compare with Eq. (5.5),

$$t_n = \frac{h_i^2 - h^2}{4 \text{ K}}$$
(5.7)

Hewson (1945) has suggested a value of 3 m² sec⁻¹ for K.

PLUME TRAPPING

Plume trapping occurs when the plume is trapped between the ground surface and a stable layer aloft. Bierly and Hewson (1962) have suggested the use of an equation that accounts for the multiple eddy reflections from both the ground and the stable layer:

$$\begin{split} &\chi\left(\mathbf{x},(\mathbf{x},\mathbf{0},\mathbf{z};\mathbf{H})=\frac{\mathbf{Q}}{2\mathbf{v}\cdot\mathbf{u}\cdot\mathbf{v}\cdot\mathbf{v}\cdot\mathbf{v}}\right\{\\ &\exp\left[-\frac{1}{2}\left(\frac{\mathbf{z}-\mathbf{H}}{\mathbf{v}_{\mathbf{v}}}\right)^{2}\right]\\ &+\exp\left[-\frac{1}{2}\left(\frac{\mathbf{z}+\mathbf{H}}{\mathbf{v}_{\mathbf{v}}}\right)^{2}\right]\\ &+\sum_{N=1}^{N}\left[\exp\left[-\frac{1}{2}\left(\frac{\mathbf{z}+\mathbf{H}-2\ NL}{\mathbf{v}_{\mathbf{v}}}\right)^{2}\right]\\ &+\exp\left[-\frac{1}{2}\left(\frac{\mathbf{z}+\mathbf{H}-2\ NL}{\mathbf{v}_{\mathbf{v}}}\right)^{2}\right]\\ &+\exp\left[-\frac{1}{2}\left(\frac{\mathbf{z}+\mathbf{H}-2\ NL}{\mathbf{v}_{\mathbf{v}}}\right)^{2}\right] \\ \end{split}$$

where L is the height of the stable layer and J = 3or a far sufficient to include the important reflection and model by assuming no effect of the stable layer until $z_{e} = 0.47$. Leve Chapter 3). It is assumed that at this distance, $2x_{e}$ unforms writch all the downwind distance, $2x_{e}$ unform writch all inclusions, and the field stars, $2x_{e}$ unform writch inclusions, and the following equation can be medite medi-

$$\chi (\mathbf{x}, \mathbf{y}, \mathbf{z}; \mathbf{H}) = \frac{\mathbf{Q}}{\sqrt{2\pi} \sigma_{y} \mathbf{L} \mathbf{u}} \exp \left[-\frac{1}{2} \left(\frac{\mathbf{y}}{\sigma_{y}} \right)^{s} \right]$$

(5.9)

For distances between x_i , and $2 x_i$, the best approximation to the ground-level centraline concentration is that read from a straight line drawn between the concentrations for points x_i , and $2 x_i$, on a log-log plot of ground-level centerline concentration as a function of distance.

CONCENTRATIONS AT GROUND LEVEL COMPARED TO CONCENTRATIONS AT THE LEVEL OF EFFECTIVE STACK HEIGHT FROM ELEVATED CONTINUOUS SOURCES

There are several interesting relationships between ground-level concentrations and concentrations at the level of the plume centerline. One of

ATMOSPHERIC DISPERSION ESTIMATES

these is at the distance of maximum concentration at the ground. As a rough approximation the maximum ground-leval concentration occurs at the distance where $\alpha_{\rm e}=\sqrt{2\rho}$ H. This approximation is much hetter for unstable conditions than for stable conditions with this approximation, the ratio of cencentration at plume centering to that at the ground is:

$$\begin{split} & \frac{\chi}{\chi(x_0,0,1)} = -\frac{\frac{1}{2} \left[1.0 + \exp{-\frac{1}{2} - \left(\frac{2it}{\pi_0}\right)^4} \right]}{\exp{-\frac{1}{2} - \left(\frac{2it}{\pi_0}\right)^4}} \\ & -\frac{\frac{1}{2} \left[1.0 + \exp{-0.5 \left(\sqrt{2}\right)^2} \right]}{\exp{-0.5 \left(\sqrt{2}\right)^2}} \\ & -\frac{\frac{1}{2} \left[1.0 + \cos{20} \right]}{\cos{20} \left[1.0 + \cos{20} \right]} \end{split}$$

This calculation indicates that at the distance of maximum ground-level concentration the concentration at plume centerline is greater by about one-third.

It is also of interest to determine the relationship hetween σ_e and H such that the concentration at ground-level at a given distance from the source is the same as the concentration at plume level. This condition should occur where:

$$\exp - \frac{1}{2} \left(\frac{H}{\sigma_s} \right)^2 - \frac{1}{2} \left[1.0 + \exp - \frac{1}{2} \left(\frac{2H}{\sigma_s} \right)^2 \right]$$

The value $H/\sigma_s = 1.10$ satisfies this expression, which can be written as $\sigma_s = 0.91$ H (see problem 10).

TOTAL DOSAGE FROM A FINITE RELEASE

The total dosage, which is the integration of concentration over the time of passage of a plume or puff, can be obtained from:

$$D_{\tau} (x, y, 0; H) = \frac{Q_{\tau}}{\pi \sigma_{\tau} \sigma_{u}} \exp \left[-\frac{1}{2} \left(\frac{y}{\sigma_{\tau}} \right)^{s} \right]$$

$$\exp \left[-\frac{1}{2} \left(\frac{H}{\sigma_{u}} \right)^{s} \right] \qquad (5.10)$$

where $D_{\gamma} = \text{total dosage, g sec } m^$ and $Q_{\gamma} = \text{total release, g}$

The e's should be representative of the time period over which the release takes place, and care about be taken to consider the x-axis along the trajectory or path of the plume or puff travel. Large errors can easily occur if the path is not known

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accurately. The estimate of this path is usually increasingly difficult with shorter release times. D_T can also be given in curie sec m⁻¹ if Q_T is in curies.

CROSSWIND-INTEGRATED CONCENTRATION

The ground-level crosswind-integrated concontration is often of interest. For a continuous elevated source this concentration is determined from Eq. (3.2) integrated with respect to y from \sim to $+\sim$ (Gifford 1960a) givine:

$$\chi_{CWI} = \frac{2}{\sqrt{2\pi}} \frac{Q}{\sigma_s u} \exp \left[-\frac{1}{2} \left(\frac{H}{\sigma_s} \right)^2 \right]$$
 (5.11)

In diffusion experiments the ground-level crosswind-integrated concentration is often determined at particular downwind distances from a crosswind line or arc of sampling measurements made at this distance. When the source strength, Q, and average wind speed, user linowing, each nuclear the set mated directly even though no measurements were made of the source of the source of the source of the directly even though no measurements were made or the source of the source of the source of the directly even though no measurements were made or the source of the source of the source of the relation of dependence of the source of

ESTIMATION OF CONCENTRATIONS FOR SAMPLING TIMES LONGER THAN A FEW MINUTES

Concentrations directly downwind from a source decrease with sampling time mainly because of a larger o, due to increased meander of wind direction. Stewart, Gale, and Crooks (1958) reported that this decrease in concentration follows a one-fifth nower law with the sampling time for sampling periods from about 3 minutes to about half an hour. Cramer (1959) indicates that this same power law applies for sampling times from 3 seconds to 10 minutes. Both of these studies were based on observations taken near the height of release. Gifford (1960h) indicates that ratios of peak to mean concentrations are much higher than those given by the above power law where observations of concentrations are made at heights considerably different from the height of release or considerably removed from the plume axis. He also indicates that for increasing distances from an elevated source, the ratios of peak to average concentrations observed at ground level approach unity. Singer (1961) and Singer, et al. (1963) show that ratios of peak to mean concentrations depend also on the stability of the atmosphere and the type of terrain that the plume is passing over. Nonhebel (1960) reports that Meade deduced a relation between calculated concentrations at ground lovel and the sampling time from "a study of published data on lateral and vertical diffusion coefficients in steady winds." These relations are shown in Table 5-1.

Table 5-1	VARIATION	OF CAU	CULATEO	CONCENTRATION
	WITH S	AMPLIN	3 TIME	

Sampling Time	Ratio of Galculated Concentration to 3-minute Concentration
3 minutes	1.00
15 minutes	0.82
1 hour	0.61
3 hours	0.51
24 hours	0.36

This table indicates a power relation with times $\chi_{a} \ll t^{-1.5}$. Note that these estimates were based upon published dispersion coefficients rather than upon sampling results. Information in the references cited indicates that effects of sampling time are exceedingly complex. If it is necessary to estitime intervals greater than a few minutes, the best estimate apparently can be obtained from:

$$\chi_s := \chi_s \left(\frac{t_k}{t_s}\right)^p \qquad (5.12)$$

where χ_{c} is the desired concentration estimate for the sampling time, t_{a_1} , χ_{c} is the concentration estinate for the shorter sampling time, t_{a_1} (probably ubout 10 minutes); and p should be hetween 0.17 und 0.2. Eq. (5.12) probably would be applied nost appropriately to sampling times less than 2 iours (see problem 19).

ESTIMATION OF SEASONAL OR ANNUAL AVERAGE CONCENTRATIONS AT A RECEPTOR FROM A SINGLE POLLUTANT SOURCE

For a source that emits at a constant rate from jour to hour and day to day, estimates of sassands *x* annual average concentrations can be made for any distance in any dimetric in it statistic wind "ross data are available for the period under study. A wind rose gives the frequency of accurance for each wind line tion (usually to 16 points) and wind usual) for the period under contaction (usual) of the period under consideration (from 11 month to 10 years). A stability wind rose stability class

If the wind directions are taken to 16 points and it is assumed that the wind directions within such sector are distributed randomly over a pariod of a month or a season, it can further be assumed that the effluent is uniformly distributed in the horizontal within the sector (Holland, 1933, p. 540). The appropriate equation for average concentration is then either:

$$\begin{split} \bar{\overline{\chi}} &= \frac{2 \ Q}{\sqrt{2\pi} \ \sigma_s \ u} \left[\frac{2\pi \ x}{16} \right] \exp \left[-\frac{1}{2} \left(\frac{H}{\sigma_s} \right)^2 \right] \\ &= \frac{2.03Q}{\sigma_s \ ux} \ \exp \left[-\frac{1}{2} \left(\frac{H}{\sigma_s} \right)^2 \right] \end{split} \tag{5.13}$$

or

$$\overline{x} = \frac{Q}{L u \left(\frac{2\pi x}{16}\right)} = \frac{2.55 Q}{L u x}$$
(5.14)

depending upon whether a stable layer aloft is affecting the distribution.

The estimation of χ for a particular direction and downrowing distances can be accoundingly by the standard structure of the standard structure of the class and solving the appropriate equation (6.13 or that a SSW wind allocit a workpoint to the MNG or a given direction and distance by semining all the constructions and winglight gash orea secondback to the structure of the structure structure of the structure of the structure of the structure structure of the structure of the structure of the structure structure of the structure of the structure of the structure structure of the structure of the structure of the structure structure of the structure of the

$$\begin{split} \chi\left(\mathbf{x},0\right) &= \sum_{\mathbf{N}} \sum_{\mathbf{N}} \left\{ \frac{2 \, \mathbf{Q} \, \left(\left(\mathbf{o},\mathbf{S},\mathbf{N}\right)\right)}{\sqrt{2 \pi} \, \sigma_{as} \, \mathbf{u}_{\mathbf{N}} \left(\frac{2 \pi \, \mathbf{x}}{16}\right)} \right. \\ &\left. \exp\left[-\frac{1}{2} \left(\frac{\mathbf{H}_{a}}{\sigma_{as}}\right)^{2}\right] \right\} \tag{5.15}$$

- where i (0, S, N) is the frequency during the period of interest that the wind is from the direction 0, for the stability condition, S, and wind speed class N.
 - a_{s0} is the vertical dispersion parameter evaluated at the distance x for the stability condition S.
 - u_N is the representative wind speed for class N.
 - H_e is the effective height of release for the wind speed u_N.

Where stability wind ross information cannot be obtained, a first-order approximation may be made of seasonal or annual average concentrations by using the appropriate wind ross in the same manner, and assuming the neutral stability class, D, only.

METEOROLOGICAL CONDITIONS ASSOCIATED WITH MAXIMUM GROUND-LEVEL CONCENTRATIONS

 For ground-level sources maximum concentrations occur with stable conditions.

- Por elevated sources maximum "intractanceut" concentrations occur with unatable conditions when particulate the source of the source of the line of the source of the source of the source has ever close to the point of emission (on the order of 10.5 stanch height). These concentrations are usually of little general interest because of their very short dumition; they connot be estimated from the material presented in this worklook.
- 3. For elevated sources maximum concentrations for time periods of a few minutes occur with unstable considerably united sources and those that the considerably under those conditions, the concentrations averaged over a few minutes are still high compared to those found under other conditions. The distance of this form it to Stuck height donwrind) and the concentration drops off mpidly downwind with increasing distance.
- 4. For elevated sources maximum concentrations for time periods of about half an hour can occur with fumigation conditions when an unstable layer increases vertically to mix downward a plume previously discharged within a stable layer. With small AH, the fumigation can occur close to the source but will be of relatively short duration. For large AH, the fumigation will occur some distance from the stack (perhaps 30 to 40 km), but can persist for a longer time interval. Concentrations considerably lower than those associated with fumigations, but of significance can occur with neutral or unstable conditions when the dispersion upward is severely limited by the existence of a more stable layer above the plume, for example, an inversion.
- 5. Under stable conditions the maximum concentrations at ground-level from objective distributed sources conditions and occur at prester distances from the source. Rowwer, the difference between mind management of the source source of the source source and a factor of 5 for file of the bulk of 20 meters and a factor of 5 for file of the bulk of 20 meters and a factor of 5 for file of the bulk of 20 meters and a factor of 5 for file of the bulk of 20 meters and a factor of 5 for file of the bulk of 20 meters and a factor of 5 for file of the bulk of 20 meters and a factor of 5 for file of the bulk of 20 meters and a factor of 5 for file of the bulk of 20 meters and a factor of 5 meters

CONCENTRATIONS AT A RECEPTOR POINT FROM SEVERAL SOURCES

Sometimes, especially for multiple sources, it is convenient to consider the receptor as being at the origin of the diffusion coordinate system. The

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source-respirate geometry can then be worked our meets by drawing or visualizing an s-axis oriented upwind (room the receptor and determining the meets) by drawing out by difficult (1996), the concentration at (0, 0, 0) from a source at (x, y, H) on a coverinate signate with the x-axis oriented uption or average and the source of the transformation from a source at (0, 0, H) on a coverinitie system with the x-axis downed (Figure 3-2). The total coverentiation is then given by summing the indconcentration is then given by summing the indsion contribution from each source (see problem

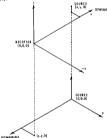


Figure 5-2. Comparison of source-oriented and receptororiented coordinate systems.

It is often difficult to determine the atmospheric conditions of wind direction, wind speed, and stability that will result in the maximum combined concentrations from two or more sources; drawing isopleths of concentration for various wind speeds and stabilities and orienting these according to wind direction is one approach.

AREA SOURCES

In dealing with diffusion of air pollutants in areas having large numbers of sources, e.g., as in urban areas, there may be too many sources of most atmospheric contaminants to consider each source

individually. Often an approximation can be mada by combining all of the emissions in a given area and treating this area as a source having an initial horizontal standard deviation, and A virtual distance, x₂₂ can then be found that will give this standard deviation. This is just the distance that will yield the appropriate value for oy from Figure Values of x, will vary with stability. Then 3-2. equations for point sources may be used, determining q. as a function of x + x., a slight variation of the suggestion by Holland (1953). This procedure treats the area source as a cross-wind line source with a normal distribution, a fairly good approximation for the distribution across an area source. The initial standard deviation for a square area source can be approximated by $\sigma_{ve} \simeq s/4.3$, where s is the length of a side of the area (see problem 221

If the emissions within an area are from varying effective stack heights, the variation may be approximated by using $\sigma_{\rm em}$. Thus H would be the score affective height of releases and $\sigma_{\rm em}$ the standard deviation of the initial vertical distribution of sources. A vitrual distance, $s_{\rm es}$ can be found, and point source sequations used for estimating concentations, determining $\sigma_{\rm es}$ as a function of $x + x_{\infty}$.

TOPOGRAPHY

Under conditions of irregular topography the direct application of a standard dispersion equation is often invalid. In some situations the best one may be able to do without the benefit of *in situ* experiments is to estimate the upper limit of the concentrations likely to occur.

For example, to calculate concentrations on a billide downwind from and facing the source and at about the effective source height, the equation for concentrations at ground-level from a groundlevel source (Eq. 3.4) will yield the highest expected concentrations. This would closely approximatic the attantion under stable conditions, when bounder that hilling. Under mathails conditions the flow is more likely to rise over the hill (see problem 21).

With downalope flow when the receptor is at a lower elevation than the source, a likely assumption is that the flow parallels the slope; i.e., no allowance is made for the difference between groundlevel elevations at the scence and at the recentor.

Where a steep ridge or bluff restricts the horizontal dispersion, the flow is likely to be parallel to such a bluff. An assumption of complete reflection at the bluff, similar to eddy reflection at the ground from an elevated source, is in order. This may be accomplished by using:

$$\chi (\mathbf{x}_{ij}, \mathbf{0}_{i}^{*}\mathbf{H}) = \frac{\mathbf{Q}}{\pi \sigma_{j} \sigma_{ij} \mathbf{u}} \left\{ \exp \left[-\frac{1}{2} \left(\frac{\mathbf{y}}{\sigma_{j}} \right)^{*} \right] \right\} \\ + \exp \left[-\frac{1}{2} \left(\frac{2 \operatorname{By}}{\sigma_{j}} \right)^{*} \right] \right\} \left\{ \exp \left[-\frac{1}{2} \left(\frac{H}{\sigma_{i}} \right)^{*} \right] \right\}$$
(5.16)

B is the distance from the x-axis to the restricting bluff, and the positive y axis is defined to be in the direction of the bluff.

The restriction of horizontal dispersion by valley isdes is somewhat analogous to restriction of the vartical dispersion by a stable layer aloft. When the σ_p becomes great enough, the concentrations can be assumed to be uniform across the width of the valley and the concentration calculated according to the following equation, where in this case Y is the width of the valley.

$$\chi = \frac{2Q}{\sqrt{2\pi} \sigma_s Y u} \exp \left[-\frac{1}{2} \left(\frac{H}{\sigma_s}\right)^2\right] (5.17)$$

LINE SOURCES

Concentrations downwind of a continuously emitting infinite line source, when the wind direction is normal to the line, can be expressed by rewriting equation (12) p. 154 of Sutton (1932):

$$\chi$$
 (x,y,0;H) = $\frac{2 q}{\sqrt{2\pi} \sigma_s u} \exp \left[-\frac{1}{2} \left(\frac{H}{\sigma_s}\right)^s\right]$

(5.18)

Here q is the source strength per unit distance, for example, g sec⁺ m⁻. Note that the horizontal dispersion parameter, $_{\infty}$, does not appear in this qualton, since it is assumed that latend dispersion from one segment of the line is componented by dissegments. Also y does not appear, these concentration at a given X is the same for any value of y (see problem 23).

Concentrations from infinite line sources when the wind is not perpendicular to the line can be approximated. If the angle between the wind direction and line source is s, the equation for concentration downwind of the line source is:

$$\chi$$
 (x,y,0;H) = $\frac{2 q}{\sin \phi \sqrt{2\pi} \sigma_s u} \exp \left[-\frac{1}{2} \left(\frac{H}{\sigma_s}\right)^s\right]$

(5.19)

This equation should not be used where ϕ is less than 45° .

When estimating concentrations from finite line sources, one must account for "dege effect" cause by the out of the line source. These effects will of comme extend to prestar cross-wind distances as trations from a finite line source oriented crosswind, doften the x-axis in the distriction of the mean wind, and passing through the receptor of interest. The limits of the line source and be defined as extending from y, to y, where y, is less than y, 1889. In the limits of the line source and the distribution to the limits of the line source and the defined as extending from y, to y, where y is less than y (1889) counties (11), p. 18(s), is:

$$\begin{split} \chi \left(x, 0, 0; H \right) &= \frac{2 \ q}{\sqrt{2 \pi} \ \sigma_{x} \ 1} \ \text{ org} \left[-\frac{1}{2} \left(\frac{H}{\sigma_{x}} \right)^{2} \right] \\ \int_{p_{1}}^{p_{2}} \frac{1}{\sqrt{2 \pi}} \ \exp \left(-0.5 \ p^{3} \right) \ dp \qquad (5.20) \\ \text{ where } p_{1} - \frac{y_{1}}{y_{1}} \ p_{2} - \frac{y_{1}}{y_{1}} \end{split}$$

The value of the integral can be determined from tabulations given in most statistical tables (for example, see Burrington (1953), pp. 273-276; also see problem 24).

INSTANTANEOUS SOURCES

Thus far we have considered only sources that were emitting continuously or for time periods equal to or greater than the travel times from the source to the point of interest. Cases of instantaneous release, as from an explosion, or short-term releases on the order of seconds, are often of practical concorn. To determine concentrations at any position downwind, one must consider the time interval after the time of release and diffusion in the downwind direction as well as lateral and vertical diffusion. Of considerable importance, but very difficult, is the determination of the path or trajectory of the "puff." This is most important if concentrations are to be determined at specific points. Determining the trajectory is of less importance if knowledge of the magnitude of the concentrations for particular downwind distances or travel times is required without the need to know exactly at what points these concentrations occur. Rewriting Sutton's (1932) equation (13), p. 155, results in an equation that may be used for estimates of concentration downwind from a release from height, H:

$$\begin{array}{l} \chi\left(\mathbf{x},\mathbf{y},\mathbf{0},\mathbf{H}\right) = \frac{2}{(2\pi)^{3/2}\sigma_{0}\sigma_{1}\sigma_{1}} \exp\left[-\frac{1}{2}\left(\frac{\mathbf{x}-\mathbf{ut}}{\sigma_{n}}\right)^{2}\right] \exp\left[-\frac{1}{2}\left(\frac{\mathbf{H}}{\sigma_{n}}\right)^{2}\right] \\ \exp\left[-\frac{1}{2}\left(\frac{\mathbf{y}}{\sigma_{1}}\right)^{2}\right] \exp\left[-\frac{1}{2}\left(\frac{\mathbf{y}}{\sigma_{1}}\right)^{2}\right] \end{array}$$
(5.21)

(The numerical value of (2π)^{3/2} is 15.75.)

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The symbols have the usual meaning, with the important exceptions that Q_T represents the *total mass* of the release and the o's are *not* those evaluated with respect to the dispersion of a continuous source at a fixed point in space.

In Eq. (5.21) the s's refer to dispersion statistics following the motion of the expanding puff. The e, is the standard deviation of the concentration distribution in the puff in the downwind direction, and t is the time after release. Note that there is no dilution in the downwind direction by wind sneed. The speed of the wind mainly serves to give the downwind position of the center of the puff, as shown by examination of the exponential involving or. Wind spoed may influence the dispersion indirectly because the dispersion parameters ay, ar, and es may be functions of wind speed. The or's and on's for an instantaneous source are less than those for a few minutes given in Figure 3-2 and 3-3. Slade (1965) has suggested values for a or and a for quasi-instantaneous sources. These are given in Table 5-2. The problem remains to make best estimates of os. Much loss is known of diffusion in the downwind direction than is known of lateral and vertical dispersion. In general one should expect the or value to be about the same as or. Initial dimensions of the puff, i.e., from an explosion, may be approximated by finding a virtual distance to give the appropriate initial standard deviation for each direction. Then e, will be determined as a function of x + x,, v, as a function of x + x, and o, as a function of x + x.

Table 5-2 ESTIMATION OF DISPERSION PARAMETERS FOR DUASI-INSTANTANEOUS SOURCES (FROM SLADE, 1965)

	X 1	100 m	x =	4 km
	σ, 10	۰. 15	4, 300	220
Unstable Neutral	4	3.8	120	50
Very Stable	1.3	0.75	35	1

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Most other widely used diffusion equations are variant forms of the ones presented here. With respect to ground-level concentrations from an elevated source (Eq. 3.2):

$$\begin{split} \chi\left(x,y,0;H\right) &= \frac{Q}{\pi \sigma_{f} \sigma_{g} u} \exp\left[-\frac{1}{2}\left(\frac{y}{\sigma_{f}}\right)^{*}\right] \\ \exp\left[-\frac{1}{2}\left(\frac{H}{\sigma_{s}}\right)^{*}\right] \end{split} \tag{3.2}$$

Other well-known equations can be compared:

Basanquet and Pearson (1936):

$$\chi (\mathbf{x}, \mathbf{y}, 0; \mathbf{H}) = \frac{\mathbf{Q}}{\sqrt{2\pi} \operatorname{pq} \mathbf{x}^2 \mathbf{u}} \exp \left[-\frac{1}{2} \left(\frac{\mathbf{y}}{\mathbf{qx}} \right)^* \right] \exp \left[-\frac{\mathbf{H}}{px} \right]$$
(6.1)

where p and q are dimensionless diffusion coefficients.

Sutton (1947):

$$\begin{array}{l} _{\chi}\left(\mathbf{x}_{*}\mathbf{y}_{*}\mathbf{0};\mathbf{H}\right)=\frac{2}{\pi}\frac{Q}{C_{x}}\sum_{\mathbf{x}^{2-\alpha}}\frac{1}{\mathbf{u}} \exp\left[-\frac{1}{-\frac{1}{\mathbf{x}^{2-\alpha}}}\right]\\ \left(\frac{\mathbf{y}^{2}}{C_{x}^{2}}+\frac{H^{2}}{C_{x}^{2}}\right)\end{array} \tag{6.2}$$

.

where n is a dimensionless constant and C_r and C_s are diffusion coefficients in $m^{1/2}$.

Calder (1952):

$$\chi (x,y,0;H) = \frac{Q u}{2 k^3 a v_x^2 x^2} \exp \left[-\frac{u}{k v_x x} \left(\frac{y}{a} + H\right)\right]$$

(6.3)

where $a = \frac{v'}{w'}$, the ratio of horizontal eddy velocity to vertical eddy velocity, k is von Karman's constent approximately equal to 0.4, and $v_s = \frac{k}{\ln \frac{1}{(T_s)}}$ where z. is a roughness parameter, m. NOTE: Calder wrote the equation for the concentration at (x, y, z) from a ground-level source. For Eq. (6.3) it is assumed that the concentration at ground level from an elevated source is the same as the concentration at an elevated point from a ground-level source.

Table 6-1 lists the expressions used in these equations that are equivalent to e_y and e_z (continuous source) in this paper.

Table 6-1 EXPRESSIONS EQUIVALENT TO or AND on IN VARIOUS DIFFUSION EQUATIONS.

Equation	σ,	<i>a</i> 1
Bosanquet and Pearson	d x	√2 p x
Sutton -	1 	$\frac{1}{\sqrt{2}}$ C _x x $\frac{2\cdot n}{2}$
Calder	√2 a k v _x x u	<u>U</u>

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Other Equations



The following 26 example problems and their solutions illustrate the application of most of the techniques and equations presented in this workbook.

- PROBLEM 1: It is estimated that a burning, domp emits $3 \not\equiv sec^{-1}$ oxides of nitrogen. What is the concentration of oxide of nitrogen, averaged over approximately 10 minutes, from this source directly downwind at a distance of 3 km on an overcast night with wind speed of 7 m sec⁻¹⁹. Assume this dump to be a point round-level source with no effective rise.
- SOLJTION: Overcast conditions with a wind upsed of 7 m sec⁻¹ indicate that stability class D is most applicable (Statement, bottom of Table 3.1). For x = 3 km and stability D, $v_{-} = 100$ m from Figure 3.2 and $v_{-} = 65$ m from Figure 3.2. Reg. (3.4) for estimation of concentrations directly downwind (y = 0) from a ground-level source is a nonlicable:

$$\chi (x,0,0;0) = \frac{Q}{\pi \sigma_r \sigma_z u} = \frac{3}{\pi 190 (65) 7}$$

= 1.1 x 10⁻⁵ g m⁻² of oxides of nitrogen.

- PROBLEM 2: It is estimated that 80 g sec⁻¹ of sulfur dioxide is being emitted from a potroleum refinery from an average effective height of 60 meters. At 0800 on an overcast winter morning with the surface wind 6 m sec⁻¹, what is the ground-level concentration directly downwind from the refinery at a distance of 500 meters?
- SOLUTION: For overcast conditions, D class stability applies. With D stability at x = 500 m, n = 36 m s = 18.5 m. Using Eq. (3.3);

$$\begin{split} \chi(\mathbf{x},0,0;\mathbf{H}) &= \frac{\mathbf{Q}}{\pi \sigma_{y} \sigma_{z} \mathbf{u}} \exp \left[-\frac{1}{2} \left(\frac{\mathbf{H}}{\sigma_{z}} \right)^{2} \right] \\ &- \frac{80}{\pi 36 (18.5) 6} \exp \left[-0.5 (60/18.5)^{2} \right] \\ &- 6.37 \times 10^{-5} \exp \left[-0.5 (3.24)^{2} \right] \end{split}$$

The exponential is solved using Table A-1 (Appendix 3).

--- 6.37 x 10⁻³ (5.25 x 10⁻⁶) y --- 3.3 x 10⁻³ g m⁻⁶ of SO₆

PROBLEM 3: Under the conditions of problem 2, what is the concentration at the same distance downwind but at a distance 50 metera from the x-axis? That is: χ (500, 50, 0; 60) — ?

SOLUTION: Using Eq. (3.2):

$$\begin{split} \chi\left(x,y,0;H\right) &= \frac{Q}{\pi \sigma_{y} \sigma_{z} u} \exp\left[-\frac{1}{2} \left(\frac{y}{\sigma_{y}}\right)^{2}\right] \\ \exp\left[-\frac{1}{2} \left(\frac{H}{\sigma_{z}}\right)^{2}\right] \end{split}$$

All hut the exponential involving y has been found in the preceding problem. Therefore:

$$\chi$$
 (500, 50, 0; 60) = 3.3 x 10⁻⁵
exp [--0.5 (50/36)⁺]
= 3.3 x 10⁻⁵ (0.381)

= 1.3 x 10⁻¹ g m⁻¹ of SO,

- PROBLEM 4: A power plant humra 10 toos per hour of cost costanting 3 present suffer: the autory summer discount with the sufficient hours ground a sufficient sufficient sufficient hours ground a 1 more? from the northeast. We moving an instantion has indicated that a frontal investigation sufficient sufficient mixing to 100 meters. The 1200-meter wind 3 ministion is 100 meters. The 1200-meter sufficient is the distance to the maximum dynamics of operativitient which is the constraints of sufficient dynamics of the sufficient sufficient is the distance to the maximum ground-beet operaturitient which is the constraints of
- SOLUTION: To determine the source strength, the amount of sulfur burned is: 10 tons hr⁻³ x 2000 lb ton⁻¹ x 0.03 sulfur = 600 lb sulfur hr⁻³. Sulfur has a molecular weight of 32 and combines with 0, with a molecular weight of 32; therefore for every mass unit of sulfur burned, there result two mass units of SO₂.

$$\begin{split} & Q = \frac{64 \; (\text{molecular weight of SO}_z)}{32 \; (\text{molecular weight of sulfur})} \\ & \times \; \frac{600 \; \text{lb} \; \text{hr}^{-1} \; (453.6 \; \text{g} \; \text{lb}^{-3})}{3600 \; \text{sec hr}^{-3}} \\ & - \; 151 \; \text{g} \; \text{sec}^{-3} \; \text{of SO}_z \end{split}$$

On a sumry summer distance on the insolution should be stores, From Table 3-1, storeg insolation and ran sec² winds yield class=1 stability from Figure 3-3, the distance to the point of hilly and effective height of 190 meters. From Figure 3-3 at the distance 0, and the meters. The Figure 3-3 at the distance 0, and the meters of the much less than 0.47 L. Therefore, at this distance, the limit of mixing of 1300 meters. Point Figure 3-9, the maximum yor/Q for B stability and this effective height of 150 m in 7.5 x 10⁻⁷.

$$\chi_{sax} = \frac{\chi u}{Q_{max}} \frac{Q}{u} = \frac{7.5 \times 10^{-6} \times 151}{4}$$

= 2.8 × 10⁻⁴ g m⁻⁴ of SO₅

PROBLEM 5: For the power plant in problem 4, at what distance does the maximum ground-

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level concentration occur and what is this concentration on an overcast day with wind speed 4 m sec"'?

SOLUTION: On an overcost day the stability class would be D. From Figure 3-9 for D stability and H of 150 m, the distance to the point of maximum ground-level concentration is 5.6 km, and the maximum gu/Q is 3.0 x 10⁻⁹.

$$\chi_{max} = \frac{3.0 \times 10^{-4} \times 151}{4}$$

= 1.1 × 10^{-4} c m⁻³

- PROBLEM 6: For the conditions given in problem 4, draw a graph of ground-level centerline sulfur dioxide concentration with distance from 100 meturs to 100 km. Use log-log graph paper.
- SOLUTION: The frontal inversion limits the mixing to L = 1500 moters. The distance at which $\sigma_a = 0.47$ L = 706 m is $x_c = 5.6$ km. At distances less than this, Eq. (3.3) is used to calculate concentrations:

$$\chi$$
 (x,0,0;H) = $\frac{Q}{\pi \sigma_{\Gamma} \sigma_{z} u} \exp \left[-\frac{1}{2} \left(\frac{H}{\sigma_{x}}\right)^{z}\right]$

At distance equal to or greater than 2 x₁₀ which is 11 km, Eq. (3.5) is used:

$$\chi (x,0,0;H) = \frac{Q}{\sqrt{2\pi} \sigma_r L u}$$

Solutions for the equations are given in Table 7-1. The values of concentration are plotted against distance in Figure 7-1.

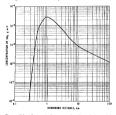


Figure 7-1. Concentration as a function of downwind distance (Problem 6).

Table 7-1 CALCULATION OF CONCENTRATIONS FOR VARIOUS DISTANCES (PROBLEM 6)

x, km	u, m sec=s	a _y , m	σ _e , n	H/ø	$\exp\left[-\frac{1}{2}H/\sigma\right]$	ν ^{]α}] ⁸ ^{10,13}
0.3	4	52	30	5.0	3.73 x 10-e	2.9 x 10**
0.5	4	83	51	2.94	1.33 x 10 ⁻²	3.8 x 10->
0.8	4	129	85	1.77	0.209	2.3 x 10-*
1.0	4	157	110	1.36	0.397	2.8 x 10**
2.0	4	295	230	0.65	0.810	1.4 x 10-*
3.0	4	425	365	0.41	0.919	7.1 x 10 *
5.5	4.5	720	705	0.21	0.978	2.1 x 10 ⁻³
x, km	u, m sec->	<i>е</i> ът т	L, m			8 m ⁻¹
11.0	4.5	1300	1500			6.9 x 10 ···
30	4.5	3000	1500			3.0 x 10 *
100	4.5	8200	1500			1.1 x 10-*

- PROBLEM 7: For the conditions given in problem 4, draw a graph of ground-level concentration versus crosswind distance at a downwind distance of 1 km.
- SOLUTION: From problem 4 the ground-lovel conterline concentration at 1 km is 2.8 x 10⁻⁴ g m⁻³. To determine the concentrations at distances y from the x-axis, the ground-lovel conterline concentration must be multiplied by the

factor exp
$$\left[-\frac{1}{2} \left(\frac{y}{\sigma_y} \right)^s \right]$$

 $\sigma_y = 157$ meters at x = 1 km. Values for this computation are given in Table 7-2.

Table 7-2 DETERMINATION OF CROSSWIND CONCENTRATIONS (PROBLEM 7)

y. m	$-\frac{y}{\sigma_y}$	$\exp\left[-\frac{1}{2}\left(\frac{y}{\sigma_y}\right)^2\right]$	χ (x,y,0)
± 100	0.64	0.815	2.3 x 10 *
± 200	1.27	0.446	1.3 x 10 ⁻¹
± 300	1.91	0.161	4.5 x 10 ⁻⁰
± 400	2,55	3.87 x 10-*	1.1 x 10 →
± 500	3.18	6.37 x 10 ^{-a}	1.8 x 10

These concentrations are plotted in Figure 7-2.

- PROBLEM 3: For the conditions given in problem 4, determine the position of the 10⁻³ g m^{-a} ground level incpleth, and determine its area.
- SOLUTION: From the solution to problem 6, the graph (Figure 7-1) shows that the 10^{-5} g m⁻³ isopleth intersects the x-axis at approximatoly x = 350 meters and x = 8.6 kilometers.

ATMOSPHERIC DISPERSION ESTIMATES

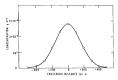


Figure 7-2. Concentration as a function of crosswind distance (Problem 7).

The values necessary to determine the isopleth half widths, y, are given in Table 7-3.

Table 7-3	DETERMINATION OF ISOPLETH WIDTH	S
	(PROBLEM 8)	

x, km	су. т	χ icenterlinel, g m ⁻ⁿ	$\frac{\chi}{\chi}$ (isopleth) $\frac{\chi}{\chi}$ (contertine)	γ/σ_y	5, N
0.5	83	3.8 x 10 ^{-a}	0.253	1.64	135
0.8	129	2.3 × 10 ⁻⁴	4.35 x 10 ²	2.50	323
1.0	157	2.8 x 10-4	3.53 x 10 ²	2.59	407
2.0	295	1.4 x 10 ⁻⁴	7.14 x 10 ^{-s}	2.30	679
3.0	425	7.1 x 10 ⁻⁶	1.42 x 10~1	1.98	843
4.0	540	4.0 x 10 ^{-s}	0.250	1.67	933
5.0	670	2.4 x 10 ^{-s}	0.417	1.32	884
6.0	780	1.8 x 10 ⁻⁶	0.556	1.08	843
7.0	890	1.4 x 10 ^{-a}	0.714	0.82	730
8.0	980	1.1 x 10 ⁻⁵	0.909	0.44	433

The orientation of the x-axis will be toward 225° close to the source, curving more toward 210° to 215° azimuth at greater distances because of the change of wind direction with height. The isopleth is shown in Figure 7-3.

Since the isopleth approximates an ellipse, the area may be estimated by τ ab where a is the semimajor axis and b is the semiminor axis.

Example Problems

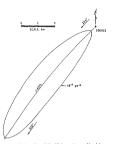


Figure 7-3. Location of the 10⁻⁹ g m⁻⁹ ground-level isopleth (Problem 8).

- PROBLEM 9: For the conditions given in problem 4, determine the profile of concentration with height from ground level to z = 450 meters at x = -1 km, y = 0 meters, and draw a graph of concentration against height above ground.
- SOLUTION: Eq. (3.1) is used to solve this problem. The exponential involving y is equal to 1. At x - 1 km, σ_r = 157 m, σ_s = 110 m. (From problem 4).

$$\frac{Q}{2\pi g_{\pi} g_{\pi} g_{\pi}} = \frac{151}{2\pi 157 (110) 4} = 3.5 \times 10^{-6} g m^{-3}$$

Values for the estimation of $\chi(z)$ are given in Table 7-4.

- PROBLEM 10: For the conditions given in problem 4, determine the distance at which the ground-level centerine concentration equals the centerline concentration at 150 meters above ground. Verify by computation of <u>x</u> (x,0,0) and <u>x</u> (x,0,150).
- SOLUTION: The distance at which concentrations at the ground and at plume height are equal should occur where $\sigma_z = 0.21$ H (See Chapter 5). For B stability and H = 150 m, $\sigma_z = 0.21$ (160) = 136 m occurs at x = 1.2 km. At this islance $\sigma_z = 181$ m.

а.	b.	с.	d.	e.	1.	8
4 0	-2-81 -9% CHD	$-\frac{1}{2}\left(\frac{2N}{\alpha_k}\right)$	2] <u>2+8</u> #4	$\operatorname{Exp}\left[-\frac{1}{2}\left(\frac{z+z}{\sigma_{1}}\right)\right]$	")"] «	+ e. X ^(d) , g m ⁻²
0	-1.36	0.397	1.36	0.397	0.794	2.78 x 10-4
30		0.552	1.64	0.261	0.813	2.85 x 10-4
60	-0.82	0.714	1.91	0.161	0.875	3.06 x 10~4
90	0.55	0.860	2.18	0.0929	0.953	3.34 x 10~4
120	0.27	0.964	2.45	0.0497	1.014	3.55 x 10-4
150	0.0	1.0	2.73	0.0241	1.024	3.58 x 10-*
180	0.27	0.964	3.00	1.11 x 10-2	0.975	3,41 x 10~4
210	0.55	0.860	3.27	4.77 x 10-*	0.865	3.03 x 10-4
240	0.82	0.714	3.54	1.90 x 10-a	0.716	2.51 x 10-*
270	1.09	0.552	3.82	6.78 x 10-4	0.553	1.94 x 10-4
300	1.36	0.397	4.09	2.33 x 10-+	0.397	1.39 x 10-4
330	1.64	0.261	4.36	7.45 x 10-*	0.261	9.14 x 10~°
360	1.91	0.161	4.64	2.11 x 10 ^x	0.161	5.64 x 10-*
3 90	2.18	0.0929	4.91	5.82 x 10 ^{-e}	0.093	3.26 x 10-*
420	2.45	0.0497	5.18	1.49 x 10™	0.050	1.75 x 10-+
450	2.73	0.0241	5.45	3.55 x 10 ¹	0.021	8.40 x 10-4

Table 7-4 DETERMINATION OF CONCENTRATIONS FOR VARIOUS HEIGHTS (PROBLEM 9)

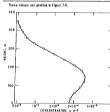


Figure 7-4. Concentration as a function of height (Problem 9).

Verifying:

$$\begin{array}{l} \left({\rm x},0,0 \right) = \frac{Q}{\pi \, \sigma_{\rm y} \, \sigma_{\rm x} \, u} \, \exp \left[{-\frac{1}{2} \left({\frac{{\rm H}}{\sigma_{\rm x}}} \right)^{\rm x}} \right] \\ = \frac{151}{\pi \, 181 \, (136) \, 4} \, \exp \left[{-\frac{1}{2} \left({\frac{150}{136}} \right)^{\rm x}} \right] \end{array}$$

$$\begin{array}{l} -4.88 \times 10^{-1} \exp\left[-\frac{1}{2} \left((1.10)^{1}\right) \\ -4.88 \times 10^{-1} (0.546) \\ -2.7 \times 10^{-1} g \, m^{-1} \end{array}\right. \\ \left. + \exp\left[-\frac{1}{2\pi s_{1}} \left\{ \exp\left[-\frac{1}{2} \left(\frac{x-H}{s_{1}}\right)^{2}\right] \right\} \\ - \frac{151}{2\pi s 11} \left(1360 + \left\{ \exp\left[-\frac{1}{2} \left(\frac{1}{136}\right)^{2}\right] \\ + \exp\left[-\frac{1}{2} \left(\frac{130}{136}\right)^{2}\right] \right\} \\ - \frac{244 \times 10^{-1} \left\{ 1.0 + \exp\left[-\frac{1}{2} \left(2.21\right)^{2}\right\} \right\} \\ - 2.44 \times 10^{-1} \left(1.0 + \exp\left[-\frac{1}{2} \left(2.21\right)^{2}\right] \right\} \\ - 2.44 \times 10^{-1} \left(1.0 + 80 \times 10^{-1}\right) \\ - 2.44 \times 10^{-1} \left(1.0 \times 10^{-1}\right) \\ - 2.44 \times 10^{-1}$$

- PROBLEM 11: For the power plant in problem 4, what will the maximum ground-level concentration be beneath the plume centerline and at what distance will it occur on a clear night with wind speed 4 m sec⁻?
- SOLUTION: A clear night with wind speed 4 m sec⁻³ indicates B stability conditions. From Ngure 3-9, the maximum concentration should occur at a distance of 13 km, and the maximum χ_0/Q is 1.7 x 10⁻⁶

$$\chi_{max} = \frac{\chi u}{Q} \times \frac{Q}{u} = \frac{1.7 \times 10^{-6} \times 151}{4}$$

= 6.4 × 10⁻⁴ g m⁻³ of SO,

- PROBLEM 12: For the situation in problem 11, what would the fumigation concentration he the next morning at this point (x - 13 km) when superadiabatic lapse rates extend to include most of the plume and it is assumed that wind speed and direction remain unchanged?
- SOLUTION: The concentration during fumigation conditions is given by Eq. (5.2) with the exponential involving y equal to 1. in this problem.

$$\chi_{\mathbf{r}} (\mathbf{x}, 0, 0; \mathbf{H}) = \frac{\mathbf{Q}}{\sqrt{2\pi} \mathbf{u} \sigma_{\mathbf{r}\mathbf{r}} \mathbf{h}_{\mathbf{i}}}$$

For the stable conditions, which were assumed to be class E, at x = 13 km, $\sigma_r = 520 \text{ m}$, and $\sigma_r = 90 \text{ m}$. Using Eq. (.5.3) to solve for h; h_i = H + 2 $\sigma_r = 150 + 2$ (90) - 330 m. From the horizontal spreading suggested by Eq. (.5.4):

$$\sigma_{\gamma F} = \sigma_{\gamma} \text{ (stable)} + \text{H/8} = 520 + 19 - 53$$

 $\chi_{F} = \frac{151}{\sqrt{2\pi} 4 \text{ (539) } 330}$
 $= 8.5 \times 10^{-6} \text{ g m}^{-3} \text{ of SO}_{\alpha}$

Note that the furnigation concentrations under these conditions are about 1.3 times the maximum ground-level concentrations that occurred during the night (problem 11).

- DROBLEMA 13: An air sampling station is located as an arbund of 2003 from a centent plant 1 at airstance of 1500 meters. The centent plant raleases fine particulates (less than 15 micross diameter) at the rate of 750 peareds per hour from 8 0-meter atack. What is the centribution from the censent plant to the total ausymded particulate concentration at the sampling station when the wind is from 30° at 3 m sec⁻¹ on a clear day in the late fails at 10007
- SOLUTION: For this season and time of day the C class stability should apply. Since the sampling station is off the plume axis, the x and y distances can be calculated:

The source strength is:

$$Q = 750 \text{ lb hr}^{-1} \ge 0.126 \frac{\text{g sec}^{-1}}{\text{lb hr}^{-1}} = 94.5 \text{ g sec}^{-1}$$

At this distance, 1489 m, for stability C, $\sigma_r =$ 150 m, $\sigma_a = 87$. The contribution to the concentration can be calculated from Eq. (3.2):

$$\begin{split} \chi(s_{2}h(H) &= \frac{-\varphi_{e_{1}}\varphi_{e_{1}}}{\Psi_{e_{1}}}\exp\left[-\frac{1}{2}\left(\frac{Y}{\varphi_{e_{1}}}\right)^{2}\right] \\ &= \frac{44.6}{r+10}\left[\frac{44.6}{r+10}\right]^{2} \\ &= \frac{44.6}{r+100}\left[\frac{1}{2}\left(\frac{Y}{2}\right)^{2}\right] \\ &= \frac{1}{2}\left[\frac{44.6}{r+10}\right]^{2} \\ &= \frac{1}{2}\left[\frac{1}{2}\left(\frac{Y}{2}\right)^{2}\right] \\ &=$$

PROBLEM 14: A proposed source is to emit 72 a sec⁻¹ of SO₂ from a stack 30 meters high with a diameter of 1.5 meters. The offluent gases are emitted at a temperature of 250°F (394°K) with an exit velocity of 13 m sec⁻¹. Flot on loglog paper a graph of maximum ground-level

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concentration as a function of wind spece. Or stability classes B and D. Datermine the critical wind speed for these stabilities, i.e., the wind speed that results in the highest concentrations. Assume that the design atmospheric pressure is 970 mb and the design atmospheric subscription is 20°C (239°K).

SOLUTION: Using Holland's effective stack height equation:

$$\begin{split} H &= \frac{-\gamma_{\rm e}}{u} \left[1.5 + 2.68 \times 10^{-\gamma_{\rm e}} \, \frac{T_{\rm e}}{T_{\rm e}} \, d \right] \\ &= \frac{13}{u} \left(1.5 + 2.68 \times 10^{-\gamma_{\rm e}} \, 870^{-\gamma_{\rm e}} \right) \\ &\left(\frac{394 + 283}{384} \right) \, (1.5) \right] \\ &= \frac{19.6}{u} \left[1.5 + 2.6 \left(\frac{101}{384} \right) \, 1.5 \right] \\ &= \frac{19.6}{u} \left(1.5 + 2.6 \left(0.256 \right) \, 1.5 \right] \\ &= \frac{19.6}{u} \left(1.5 + 1.0 \right) \\ &= \frac{19.6}{u} \left(2.5 \right) \\ &= \frac{19.6}{u} \\ &= \frac{19.6}{u} \\ &= \frac{19.6}{u} \\ &= \frac{19.6}{u} \\ \end{aligned}$$

The effective stack heights for various wind speeds and stabilities are summarized in Table 7-5.

Table 7-5	EFFECTIVE	STACK	HEIGHTS	(PROBLEM	14)
-----------	-----------	-------	---------	----------	-----

	Class D		Class 8		
и, m secL	дH, m	h + ΔH, m	1.15 ДН, M	h + 1.15 дН, m	
0.5	97.6	127.6	112.2	142.2	
1.0	48.8	78.8	56.1	86.1	
1.5	32.6	62.6	37.5	67.5	
2	24.4	54.4	28.1	58.1	
3	16.3	46.3	18.7	48.7	
5	9.8	39.8	11.3	41.3	
7	7.0	37.0	8.0	38.0	
10	4.9	34.9			
20	2.4	32.4			

By use of the appropriate height, H, the maximum concentration for each wind speed and stability can be determined by obtaining the

maximum χ_U/Q as a function of H and stability from Figure 3-9 and multiplying by the appropriate Q/u. The computations are summarized in Table 7-6, and platted in Figure 7-5.

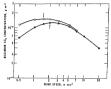


Figure 7-5. Maximum concentration as a function of wind speed (Problem 14),

Table 7-6 MAXIMUM CONCENTRATION AS A FUNCTION OF WIND SPEED (PROBLEM 14)

Stability Class	0, m sec-1	H, m	χ ^{10/0} 6055 ²	0/u, g m-s	Xuer g m-s
В	0.5	142.2	8.0 x 10 ^{-e}	144	1.15 x 10-*
	1.0	86.1	2.0 x 10-*	72	1.44 x 10 ^{-a}
	1.5	67.5	3.1 x 10 ^{-s}	48	1.49 x 10-*-€
	2	58.1	4.1 x 10 ^{-s}	36	1.48 x 10 ⁻³
	3	48.7	5.7 x 10 ^{-s}	24	1.37 x 10 ⁻⁹
	5	41.3	7.8 x 10 ⁻¹	14.4	1.12 × 10-*
	7	38.0	8.7 x 10⊸	10.3	8.96 x 10 *
0	0.5	127.6	4.4 x 10-e	144	6.34 x 10 ⁻⁴
	1.0	78.8	1.42x10-4	72	1.02 x 10 ³
	1.5	62.6	2.47x10-s	48	I.19 x 10 ^{-a}
	2	54.4	3.5 x 10~5	36	1.26 x 10 - ↔
	3	46.3	5.1 x 10-*	24	1.22 x 10 ⁻⁵
	5	39.8	7.3 x 10-s	14.4	1.05 x 10-*
	7	37.0	8.2 x 10™	10.3	8.45 x 10™
	10	34.9	9.4 x 10 ^{-s}	7.2	8.77 x 10 ⁴
	20	32.4	1.1 x 10⁻₄	3.6	3.96 x 10-*

The wind speeds that give the highest maximum concentrations for each stability are, from Figure 7-5: B 1.5, D 2.0.

PROBLEM 15: A proposed pulp processing plant is expected to emit ¼ ton per day of hydrogen sulfide from a single stack. The company property extends a minimum of 1800 meters from the proposed location. The nearest receptor

is a small town of 500 inhabitants 1700 meters northeast of the plant. Plant managers have decided that it is desirable to maintain concentrations below 20 ppb (parts per billion by volume), or approximately 2.9 x 10⁻⁵ g m⁻⁵ for any period greater than 30 minutes. Wind direction frequencies indicate that winds blow from the proposed location toward this town between 10 and 15 per cent of the time. What height stack should be erected? It is assumed that a design wind speed of 2 m sec-1 will be sufficient, since the effective stack rise will be quite great with winds less than 2 m avr1 Other than this stipulation, assume that the physical stack height and effective stack height are the same, to incorporate a slight safety factor.

SOLUTION: The source strength is:

From Eq. (4.2):

$$\sigma_r \sigma_z = \frac{0.117 \text{ Q}}{\chi_0 \text{ u}} = \frac{0.117 (5.25)}{(2.9 \times 10^{-3}) 2}$$

- 1.06 x 10⁴ m⁵

At a design distance of 1500 meters (the limit of company property), $c_r \sigma_s = 1.06 \times 10^\circ$ gives a point from Figure 4-1 about 0.2 from Class C to Class D along the line x = 1500 m. From Figure 3-3, $c_s = 30$ for this stability. $H = \sqrt{2} \alpha_s = 113$ meters

- PROBLEM 16: In problem 15 assume that the stack diameter is to be 5 ft, the temperature of the effuent 250° F, and the stack gas velocity 45 ft sec⁻¹. Form Holland's equation for effective stack height and the method used in problem 15, determine the physical stack height in the estimating ΔH_{i} use $T_{i} = 68^{\circ}$ F and p = 820mb.

$$\begin{split} & v_1 - 45 \ ft\ ee^{-\eta} = 13.7\ m\ sec^{-\eta} \\ & d - 8\ ft = -24.7\ m\ sec^{-\eta} \\ & T_1 - e8^{\eta} \ F - 20^{1/2} \ C - 394^{\eta} \ K \\ & T_2 - e8^{\eta} \ F - 20^{1/2} \ C - 394^{\eta} \ K \\ & D - 920\ mb \\ & \Delta H - \frac{v_1}{u} \ d \\ & 1.5 + 2.68\ x\ 10^{-\eta} \ \frac{T_1 - T_1}{T_n} \ d \\ & - \frac{13.7\ (2.44)}{2} \ l \\ \end{split}$$

$$= \frac{33.4}{u} [1.5 + (2.46) \ 0.256 \ (2.44)]$$

= $\frac{33.4}{u} (1.5 + 1.54)$
AH = $\frac{102}{u}$

The relation between σ_{r} σ_{r} and μ is:

$$\sigma_r \sigma_s = \frac{0.117 \text{ Q}}{\gamma_s \text{ u}} - \frac{0.117 (5.25)}{2.9 \times 10^{-6} \text{ u}} - \frac{2.12 \times 10^{4}}{\text{ u}}$$

The required computations using Figure 4-1 are summarized in Table 7-7:

Table 7-7 REQUIRED PHYSICAL STACK HEIGHT AS A FUNCTION OF WIND SPEED (PROBLEM 16)

			Stability to		₩' ==	8.00
υ,	∆⊌,	$\sigma_y \sigma_{x^i}$	Give $\sigma_y \sigma_x$ at 1500 m	$\sigma_{\theta'}$	$\sqrt{2}\sigma_{\pi}$	H'-∆H, m
m sec-5	n	m2	1500 ft	m	n	
0.5 2	04	4.24 x 104	0.9 from A to B	190	269	65
1.0 1	02	2.12 x 104	0.6 from B to C	120	170	68
1.5	68	1.41 x 10*	0.9 fram B to C	95	136	68
2.0	51	1.06 x 10+	0.2 from C to D	76	108	57
2.5	41	8.48 x 10 ^e	0.4 from C to D	64	91	50
3.0	34	7.06 x 10 ⁵	0.6 from C to D	56	79	45
5.0	20	4.24 x 10 ^a	D	42	60	40
7.0	15	3.03 x 10*	0.5 from D to E	34	48	33
10.0	10	2.12 x 10*	E	28	40	30
15.0	7	1.41 x 10°	0.5 from E to F	23	33	26

The required physical hoight is 68 meters.

- PROBLEM 17: A dispersion study is being mode over relatively open territy with facomentperticles whose size yields 1.8 x 10⁴ particles whose the study of the study of the study of the properties of the study of the deninhie to doing a particle study of the deninhie to doing a particle study of the study of the study of the study of the deninhie to doing a particle study of the study of th
- SOLUTION: The total dosage at the sampler is determined by the total sample in grams divided by the sampling rate:

$$D_r$$
 (g sec m^{-s}) = $\frac{20 \text{ particles}}{1.8 \text{ x} 10^{19} \text{ particles g}^{-1}}$

Example Problems

$$= \frac{\frac{60 \text{ sec min}^{-1}}{9 \text{ x } 10^{-6} \text{ m}^{3} \text{ min}^{-3}}}{\frac{1200}{16.9 \text{ x } 101}}$$

Dy - 7.41 x 10⁻⁶ g sec m⁻⁶

The total dosage is given in g sec m-2 from

$$D_{\tau} (x,y,0;0) = \frac{Q_{\tau}}{\pi u \sigma_{\gamma} \sigma_{z}} \exp \left[-\frac{1}{2} \left(\frac{y}{\sigma_{\gamma}}\right)^{2}\right]$$

where Q₇ is the total release in grams.

$$Q_{T} = \frac{\pi u \sigma_{y} \sigma_{x} D_{T}}{\exp \left[-\frac{1}{2} \left(\frac{y}{\sigma_{y}}\right)^{2}\right]}$$

For alightly unstable conditions (Class C) at $x = 8 \text{ km}, \sigma_y = 690 \text{ m}, \sigma_x = 310 \text{ m}; y = 2000 \text{ m},$ $u = 5 \text{ m sec}^{-1}$

$$\begin{split} Q_{\rm x} &= \frac{\pi \; 5 \; (600) \; 310 \; (7.41 \; {\rm x} \; 10^{-3})}{\exp \left[-\frac{1}{2} \left(\frac{2000}{600} \right)^2 \right]} \\ &= \frac{24.9}{\exp \left[-0.5 \; (2.90)^2 \right]} \\ &= \frac{24.9}{1.49 \; {\rm x} \; 10^{-4}} \end{split}$$

 $Q_T = 1670 \text{ g}$

Therefore

No correction has been made for the facts that the release is for 1 hour and the standard deviations represent time periods of 3 to 15 minutes.

- PROBLEM 18: A release of 2 kg of fluorescont particles is made hased on the results of the class of extension is problem 17. The conditions are class of extainly and wind speed 5 m set⁻¹. The crosswind-integrated ground-level desage along the 3-km are is determined from the samplers along this are to be 8.2 x 10⁻⁹ g sec m⁻¹. What is the effective, s, for this run?
- SOLUTION: The crosswind-integrated dosage is given by:

$$D_{OW4} = \frac{2 Q_F}{\sqrt{2 \pi} \sigma_4 u} \exp \left[-0.5 \left(\frac{H}{\sigma_4}\right)^2\right]$$

Since the source is at ground-level, the exponential has a value of 1. Solving for σ_t :

$$\sigma_{n} = \frac{2 Q_{n}}{\sqrt{2\pi} D_{corr} u} \\ - \frac{2 (2000)}{\sqrt{2\pi} (0.82) 5} \\ = \frac{4000}{10.28} \\ \sigma_{n} = -389 \text{ m}$$

- PROBLEM 19: At a point directly downwind from a ground-level source the 3- to 15-minute concentration is estimated to he 3/4 x 10⁻⁴ g m⁻³. What would you estimate the 2-hour concentration to be at this point, assuming no change in stability or wind velocity?
- SOLUTION: Using Eq. (5.12) and letting k 3 min, s - 2 hours, and p - 0.2:

$$\begin{array}{l} z \ _{\rm burr} = \left(\frac{8}{120} \right)^{0.2} & 3.4 \ {\rm x} \ 10^{-6} \\ \\ - \frac{1}{40}^{\frac{6}{12}} & (3.4 \ {\rm x} \ 10^{-8}) \\ \\ - \frac{3.4 \ {\rm x} \ 10^{-3}}{2.09} = 1.6 \ {\rm x} \ 10^{-6} \ {\rm g} \ {\rm m}^{-2} \end{array}$$

Letting k 15 min, s - 2 bours, and p - 0.17

$$\begin{split} \chi_{T} _{1 \text{ tore }} &= \left(\frac{16}{120}\right)^{\alpha_{1T}} 3.4 \times 10^{-s} \\ &= \frac{1}{8 \, \text{str}} \quad (3.4 \times 10^{-s}) \\ &= \frac{3.4 \times 10^{-s}}{1.42} = 2.4 \times 10^{-s} \, \text{g m}^{-s} \end{split}$$

The 2-hour concentration is estimated to be between $1.6 \ge 10^{-2}$ and $2.4 \ge 10^{-3}$ g m⁻³.

- PROBLEM 20: Two sources of SO, are shown as points A and B is Figure 7-6. On a sumy aurmore afternoon the anthrac wind is from 60° 1400 zero (SO, from two stacks whose physical heights is 120 meters and whose abit, from Hdimark equation, is Alf (m) = 638 (m sec.)/u (m sec.), fources B is a referry conting 126 ger (m sec.), fources B is a referry conting 126 ger (m sec.), source B is a referry conting 126 ger (m sec.), source B is a referry conting 126 ger (m sec.), source B is a referry conting 126 ger (m sec.), source B is a referry conting 126 ger (m sec.), source B is a referry conting 126 ger (m sec.), source B is a referry conting 126 ger (m sec.), and hence are no other sources of SO, how in the mean field of the reseptor how in the figure?
- SOLUTION: Calculate the affective height of Source A using the observed wind speed at 160 meters.

$$\Delta H = \frac{538}{8.5} = 63.3$$

 $H_A = 120 + 63 = 183 \text{ m}$
 $Q_A = 1450 \text{ g sec}^{-1}$
 $H_B = 60 \text{ m}$
 $Q_B = 126 \text{ g sec}^{-1}$

For a summy summer afternoon with wind speed 6 m sec⁻¹, the stability class to be expected is C. The equation to be used is Eq. (3.2):

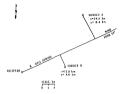


Figure 7-6. Locations of sources and receptor (Problem 20).

$$\begin{array}{l} \chi\left(xy,0;11\right) = \frac{9}{\tau_{0},\tau_{0}} \exp\left[-\frac{1}{2}\left(\frac{y}{\gamma}\right)^{2}\right] \\ \exp\left[-\frac{1}{2}\left(\frac{H}{\gamma}\right)^{4}\right] \\ \exp\left[-\frac{1}{2}\left(\frac{H}{\gamma}\right)^{4}\right] \\ For Bourse A, x = 24.6 \, \mathrm{km}, y = 8.4 \, \mathrm{km} \\ \sigma_{1} = 1120 \, \mathrm{m}, x = 1120 \, \mathrm{m}, u = 8.5 \, \mathrm{ms}\,\mathrm{er}^{-1} \\ \mathrm{sec}^{-1} = 1120 \, \mathrm{m}, u = 8.5 \, \mathrm{ms}\,\mathrm{er}^{-1} \\ \mathrm{sec}^{-1} = 1120 \, \mathrm{m}, u = 8.5 \, \mathrm{ms}\,\mathrm{er}^{-1} \\ \mathrm{sec}^{-1} = 1120 \, \mathrm{m}, u = 100 \, \mathrm{m}, u = 8.5 \, \mathrm{ms}\,\mathrm{er}^{-1} \\ \mathrm{sec}^{-1} = 1120 \, \mathrm{m}, u = 100 \, \mathrm{m}, u = 8.5 \, \mathrm{ms}\,\mathrm{er}^{-1} \\ \mathrm{sec}^{-1} = 100 \, \mathrm{m}, u = -100 \, \mathrm{m}, u = 100 \, \mathrm{m}, u = -100 \, \mathrm{m}, u = -100 \, \mathrm{m}, u = 0.5 \, \mathrm{m}, u = -10 \, \mathrm{m}\, \mathrm{sec}^{-1} \\ \mathrm{sec}^{-1} = \frac{126}{\tau \, \mathrm{sub}} \, \mathrm{Geb}(40)^{-1} \, \mathrm{esc} \, \left[-0.5 \, \left(\frac{4000}{1000}\right)^{+}\right] \\ \mathrm{esp} \left[-0.5 \, \left(\frac{600}{1000}\right)^{-}\right] \\ \mathrm{esp} \left[-0.5 \, \left(\frac{600}{1000}\right)^{-}\right] \\ \mathrm{esp} \left[-0.5 \, \left(\frac{6000}{1000}\right)^{-}\right] \\ \mathrm{esp} \left[-0.5 \, \left(\frac{6000}{1000}\right)^{-}\right] \\ \mathrm{esp} \left[-0.5 \, \left(\frac{6000}{1000}\right)^{-}\right] \\ \mathrm{seb} \left[-0.5 \, \left($$

ATMOSPHERIC DISPERSION ESTIMATES

- PROBLEM 21: A stack 15 motors high emits 3 c set: of a particular air pollutant. The serrounding terrain is relatively flat accept for a cound extends 16 motors above the stack toption of existing billiarit that can be supported on the which is the highest 4 to 15-minute concentration of this pollutarit that can be supported on the which is blowing directly from the stack toption is and its and the series of assess that and the start is and the series of assess that the two models in the series of assess that and have backing the arrival series of the solid time that an arrival series of the solid three starts and the series of a series of the solid three backing the arrival series of the solid three backing three backing three backing three backing the solid three backing three b
- SOLUTION: A clear night with 4 m sec⁻¹ indicates class E stability. Eq. (3.4) for groundlevel concentrations from a ground-level source is most applicable (See Chapter 5). At 3 km for class E, a, - 140 m, a, - 43 m.

$$x = \frac{Q}{\pi \sigma_y \sigma_x u} = \frac{3}{\pi 140 (43) 4}$$

$$x = 3.97 \times 10^{-5} \text{ g m}^{-3}$$

To determine the crosswind distance from the plume centerline to produce a concentration of $10^{-1} \circ m^{-1}$ Rg. (3.8) is used:

$$y = \left[2 \ln \frac{\chi (x,0,0)}{\chi (x,y,0)} \right]^{1/7} *_{\tau}$$

$$- \left[2 \ln \frac{3.97 \times 10^{-4}}{10^{-7}} \right]^{1/7} (140)$$

$$= (2 \ln 38^{7/1} / 140)$$

$$= 3.46 \times 1.40$$

$$= 4.84 \text{ m.}$$

$$har 0 = -\frac{4.94}{3000} = 0.1614$$

$$e = 9.2^{\circ}$$

A wind shift of 9.2° is required to reduce the concentration to 10^{-1} g m⁻¹.

- PROBLEM 22: An inventory of SQ, emissions has been conducted in an urban area by equarearea, 6000 ft (1544 molerar) on a sole. The start is a sole of the sole
 - SOLUTION: A thinly overcast night with wind speed 2.5 m sec⁻¹ indicates stability of class E.

Example Problems

(It may actually be more unstable, since this is in a built-up area.) To allow for the area source, let $\sigma_{c0} = 1524/4.3 - 354$. For class E the virtual distance, $x_7 = 8.5$ km. For x = 1624 m, $\sigma_g = 28.5$. For $x + x_g = -10.024$ m, $\sigma_g = 410$ m.

$$x = \frac{Q}{\pi \sigma_r \sigma_u u} \exp \left[-\frac{1}{2} \left(\frac{H}{\sigma_r} \right)^2 \right] \\ -\frac{6}{\pi 410 (28.5) 2.5} \exp \left[-\frac{1}{2} \left(\frac{20}{28.5} \right)^2 \right] \\ = 6.54 \times 10^{-5} (0.783)$$

- PROBLEM 23: An estimate is required of the total. hydromehon concentration 300 meters downwind of an expressive at 1730 on an overcaset day with wind apped 4 mee⁻¹. The expressive present and the wind is from the west. The measured traffic flow is 8000 vehicles per hour during thin rash hour, and the average apped of the vehicles witheles for hour. At high of the set of the set of the hour with the set of the set of the vehicle set.
- SOLUTION: The expressway may be considered as a continuous infinite line source. To obtain a source strength q in grane sec⁻¹ m⁻¹, the number of vehicles per meter of highway must be calculated and multiplied by the emission per vehicle.

 $\begin{array}{l} \label{eq:Vehicles/meter} Vehicles/meter = \\ \hline Flow (vehicles hour^{-1}) \\ \hline Average speed (mlles hour^{-1}) 1600 (m mlle^{-1}) \\ = \frac{8000}{40 \times 1600} = 1.25 \times 10^{-1} (vehicles m^{-1}) \\ \end{array}$

$$q = 1.25 \times 10^{-1}$$
 (vehicles m⁻¹) $\times 2 \times 10^{-2}$
(g sec⁻¹ vehicle⁻¹)

q = 2.5 x 10⁻⁴(g sec⁻¹ m⁻¹)

Under overcest conditions with wind speed 4 m \sec^{-1} stability class D applies. Under D, at x = 300 meters, $a_s = 12$ m. From Eq. (5.18):

$$\frac{(300,0,0;0) - \frac{2q}{\sqrt{2\pi} \sigma_{s} u}}{-\frac{2(2.5 \times 10^{-4})}{2.507 (12) 4}}$$

- -4.2 x 10⁻¹ g m⁻¹ of total hydrocarbona.
- PROBLEM 24: A line of burning agricultural wasto can be considered a finite line source 150 m long. It is at mainted that the total emission of a state of the st

that it is 1600 on a sunny fall afternoon. What is the concentration directly downwind from one end of the source?

SOLUTION: Late alternoon at this time of year implies slight insolation, which with 3 m sec⁻¹ winds yields stability class C. For C stability at x = 400 m, c. = 45 m, c. = 26 m.

$$q = -\frac{Q}{150} = -\frac{90}{150} = 0.6 \text{ g sec}^{-1} \text{ m}^{-1}$$

Eq. (5.20) is appropriate.

$$\chi (x,0,0;0) = \frac{2q}{\sqrt{2\pi} \sigma_x u} \int_{p_1}^{p_2} \frac{1}{\sqrt{2\pi}}$$

$$p_1 = \frac{y}{\sigma_y} = \frac{-75}{45} = -1.67, p_2 = \frac{y}{\sigma_y} = \frac{75}{45}$$

= +1.67

$$_{\chi}$$
 (400,0,0;0) $-\frac{2 (0.6)}{\sqrt{2\pi}(26)3} \int_{-1.67}^{+1.67} \frac{1}{\sqrt{2\pi}}$

exp (-0.5 p²) dp

- 5.6 x 10⁻³ g m⁻³

For a point downwind of one of the ends of the line:

$$p_1 = 0, p_2 - \frac{y}{\sigma_r} = \frac{160}{45} = +3.33$$

$$\chi (400,0,0;0) = 6.14 \times 10^{-3} \int_{-0}^{+3.33} \frac{1}{\sqrt{2\pi}}$$
exp (-0.5 p³) dp

exp (—0.5 p²) dp

PROMELWA 25: A core mode-down of a power rescator that has been openaing for over a year occurs at 0000, releasing 1.5 x 10° curries of atmospheres of the containment weak. This total activity can be expected to decay seconding to $\{-\frac{1}{\sqrt{2}}, -^{-1}\}$: It is estimated that holds 2.5 x 10° curries of this activity is due to ioline-131, which as a half-life of 50 doys. The second holding is homispherically also be lead with a radius of 2.0 %. The accident has occurred on a relatively clear night with wind speed 2.5 m sec⁻¹. What is the concentration in the air 3 kilometers directly downwind from the source at 0400 due to all radioactive material? due to iodine-131?

SOLUTION: Source strength - leak rate x activity (corrected for decay)

Source strength of all products

$$\begin{bmatrix} t \text{ (sec)} \\ \hline t_0 \text{ (sec)} \end{bmatrix}^{-0.2}$$

- 1.74 x 10⁻² $\begin{pmatrix} t \\ 1 \end{pmatrix}^{-0.2}$

To determine decay of materials with the half-life given, multiply by $\exp\left(\frac{-0.693\ t}{L}\right)$ where t is time and L is half-life.

Source strength of I111.

$$Q_t$$
 (curies sec⁻¹) = 1.157 x 10⁻⁴ (5.3 x 10⁴) exp
 $\left(\frac{-0.693 \text{ t}}{\text{L}}\right)$

For I₁₃₁ L = 6.95 x 10^a sec

$$Q_t = 6.13 \times 10^{-4} \exp \left(\frac{-0.693 \text{ t}}{6.95 \times 10^3} \right)$$

For a clear night with wind speed 2.5 m sec⁻¹, class F applies. Approximate the spreading at the reactor shell by 2.15 $\sigma_{c0} = 2.15 \ \sigma_{c0} = 5.15 \ \sigma_{c0} = 5.15 \ \sigma_{c0} = 0.25 \ \sigma_{$

At
$$x = 3000$$
 m. $x + x_r = 3250$ m, $\sigma_r = 100$ m.
 $x + x_s = 3560$ m, $\sigma_s = 29$ m.

$$\chi$$
 (x,0,0;0) = $\frac{Q}{\pi \sigma_y \sigma_e u}$ = $\frac{Q}{\pi 100}$ (29) 2.5
- 4.4 x 10⁻⁶ Q

For concontration at 0400, 3000 m downwind due to all radioactivity, t - 7200 seconds,

$$\chi_{\Lambda} = 4.4 \text{ x } 10^{-6} (1.74 \text{ x } 10^{-3}) (7200)^{-6.3}$$

= 7.66 x 10⁻⁷ (0.17)

 $\chi_{\Lambda} = 1.3 \times 10^{-7} \text{ curies m}^{-4}$

The concentration at 0400, 3000 m downwind due to I^{143} is:

χ₁ == 4.4 x 10^{-e} (6.13 x 10⁴) exp [--0.997 x 10^{-e} (7200)]

— 2.7 x 10^{-x} (1.0) The decay of 1¹²³ is insignificant for 2 hours

x1 - 2.7 x 10⁻⁴ curies m⁻³

Table 7-8 EMERGENCY TOLERANCE LIMITS FOR UDMH VAPOR VERSUS EXPOSURE TIME

Time, minutes	Emergency Tolerance Limits, g m ^{-a}
5	1.2 × 10 ⁻²
15	8.6 x 10 ^{-z}
30	4,9 x 10 ⁻ⁿ
60	2.5 x 10 ⁻¹

What area should be evacuated?

SOLUTION: From Table 3.1, the stability class is determined to be Class F. This is not a point source but a small area source. Allowing 4.3 m_0 to equal the with of the worked area, 6.1 meters (20 foet), $e_0 \rightarrow 1.4$ meters. In attempting to determine the virtual distance, x_i , it is found to be less than 100 meters, and will be approximated by 40 meters. The release will take:

2.9 x 10³ g 1.1 x 10³ g sec⁻¹ - 2.64 x 10³ sec - 44 min.

Therefore the concentration for an exposure time of 1 hour $(2.5 \times 10^{-1} \text{ g m}^{-3})$ is of main concern.

The equation for calculation of downwind concentrations is Eq. (3.4):

 χ (x,0,0;0) = $\frac{Q}{\pi \sigma_y \sigma_z u}$ where σ_y is a function of x + x.

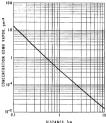
Values of the parameters and of χ are given in Table 7-9.

Example Problems

Table 7-9 DETERMINATION OF CONCENTRATION AS A FUNCTION OF DISTANCE (PROBLEM 26)

J, km	Ф _Х , Ш	x + x _y , kum	а _г . М	е ^{Ху}
0.1	2.3	0.14	5.5	13.9
0.3	5.6	0.34	12.5	2.5
0.6	9.7	0.64	22	8.2 x 10-4
1	14	1.04	35	3.6 x 10-1
3	27	3.04	93	7.0 x 10 ⁻²
6	37	6.04	175	2.7 x 10 ⁻²
10	47	10.04	275	1.4 x 10 ^{-±}

These values of χ are graphed as a function of x in Figure 7-7. The downwind concentration drops below the critical value of 2.5 x 10⁻³ at a distance of 6.5 km.



DISTANCE, km

Figure 7-7. Concentration of UDMH as a function of downwind distance (Problem 26).

Calculated widths within a given isopleth are summarized in Table 7-10.

The maximum width of the area encompassed by an isopleth is about 140 meters from the downwind position. Since the wind direction is expected to be from $310^{\circ}\pm15^{\circ}$, the sector at an azimuth of 115° to 145° plus a 140-meter rectangle on either side should be evacuated. See Figure 7-8.

Table 7-10 DETERMINATION OF WIDTHS WITHIN ISOPLETHS (PROBLEM 26)

x, kn	$x + x_{y}$ km	σ,. n	X (centerlinel, g m™s	$\frac{\chi}{\chi}$ (centerline)	<u> </u>	у. п
0.1	0.14	5.5	13.9	1.8 x 10 ⁻¹	3.55	20
Ô.5	0.54	19	1.1	2.27 x 10 ²	2.75	52
1.0	1.04	35	3.6 x 10	6.94 x 10 ^{-s}	2.31	80
2.0	2.04	66	1.3 x 10	1.92 x 10 ⁻¹	1.82	120
3.0	3.04	93	7.0 x 10 ^x	3.57 x 10™	1.44	134
4.0	4.04	120	4.8 x 10 ^{-*}	5.20 x 10 ⁻¹	1.14	137
5.0	5.04	149	3.5 x 10⁻=	7.14 x 10 ⁻¹	0.82	122
6.0	6.04	175	2.7 x 10 ²	9.26 x 10 ¹	0.39	68

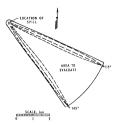


Figure 7-8. Possible positions of the 2.5 x 10^{-e} g m^{-a} isopleth and the evacuation area (Problem 26).

APPENDICES

Annendix 1: ABBREVIATIONS AND SYMBOLS

Aldereviations

cal calorie

- o, gram degrees Kelvin ° v
- motor
- m millihar ----
- record
- sec

Symbols

- ratio of horizontal eddy velocity to vertical a eddy velocity
- specific heat at constant pressure ~
- Sutton horizontal dispersion parameter Ċ,
- Ċ. Sutton vertical dispersion parameter
- inside stack diameter at stack ton d

D. (x.v.0:H) Total dosage

- 2,7183, the base of natural logarithms ~
- f (o S N) fraquency of wind direction for a given stability and wind speed class
- physical stack height ١.
- beight of the base of an inversion ь
- H effective height of emission
- H. effective height of emission for a particular wind speed
- von Karman's constant, approximately equal 1. to 0.4
- к eddy diffusivity
- two uses: 1. the height of an air layer that is relatively stable compared to the lever beneath it: a lid
 - 2, the half-life of a radioactive material
- Sutton's exponent
- an index for wind speed class N
- three uses: 1. Bosanquet's horizontal disperр sion parameter
 - 2. atmospheric pressure
 - 3, a dummy variable in the coustion for a Gaussian distribution.
- two uses: 1. Bosanquet's vertical dispersion a narameter
 - 2. emission rate per length of a line source
- emission rate of a source 0
- Q7 total emission during an entire release
- net rate of sensible heating of an air column R by solar radiation
- the length of the edge of a square area source e
- an index for stability
- a short time period

- time required for the mixing layer to develop ŧ., from the top of the stack to the top of the nlume
- a time period t.
- ambient air temperature T.
- stack gas temperature at stack top т.
- wind sneed
- a mean wind speed for the wind speed class N. u.
- horizontal eddy velocity
- stack gas velocity at the stack top v.,
- a velocity used by Calder ٧.
- w vertical eddy velocity
- distance downwind in the direction of the mean wind
- design distance, a particular downwind distance used for design purposes
- the distance at which $\sigma_{\rm c} = 0.47 L$ χ.
- a virtual distance so that $\sigma_{1}(\mathbf{x}_{1})$ equals the initial standard deviation and
- a virtual distance so that $a_{i}(\mathbf{x}_{i})$ equals the inix. tial standard deviation. e...
- a virtual distance so that g. (x.) equals the ini-Υ. tial standard deviation. g
- v crosswind distance
- height above ground level
- roughness natameter z.,
- 20 the rate of change of potential temperature 87 with height
- ΔĦ the rise of the plume centerline above the stack top
- two uses: 1, wind direction azimuth or sector 2. potential temperature
- 3 1416
- ambient air density 0.4
- the standard deviation of azimuth (wind direce i tion) as determined from a wind vane or bidirectional yone
- the standard deviation of wind elevation angle σu: as determined from a bi-directional vane
- the standard deviation in the downwind direcσ. tion of a puff concentration distribution
- on initial downwind standard deviation dire.
- the standard deviation in the crosswind direcα. tion of the plume concentration distribution
- an initial crosswind standard deviation σ_{210}
- the standard deviation in the vertical of the plume concentration distribution
- an effective s, equal to 0.8 L m
- an initial vertical standard deviation σ_{m}
- the vertical standard deviation of the plume e concentration at a particular downwind distance for the stability, S.

- s the angle between the wind direction and a line source
- χ concentration
- xcm1 crosswind-integrated concentration
- χ_d a ground-level concentration for design purposes
- xr inversion break-up fumigation concentration
- χ_k concentration measured over a sampling time, t_k
- Xuan maximum ground-level centerline concentration with respect to downwind distance

 χ_s concentration measured over a sampling time, t_s

 $\frac{\chi}{Q}$ relative concentration

- $\frac{\chi u}{Q}$ relative concentration normalized for wind speed
- x (x,y,z;H) concentration at the point (x, y, z) from an elevated source with effective height, H.
- χ (x, θ) the long-term average concentration at distance x, for a direction θ from a source.

Appendix 2: CHARACTERISTICS OF THE GAUSSIAN DISTRIBUTION

The Gaussian or normal distribution can be depicted by the bellahaped curve shown in Figure A-1. The equation for the ordinate value of this curve is:

$$y = -\frac{1}{\sqrt{2\pi \sigma}} \exp \left[-\frac{1}{2} \left(-\frac{x-x}{\sigma}\right)^2\right]$$
 (A.1)

Figure A-2 gives the ordinate value at any distance from the center of the distribution (which occurs at x). This information is also given in Table A-1. Figure A-3 gives the area under the Gaussian curve from $-\infty^{-1}$ to a particular value of p where p =



This area is found from Eq. (A.2):

Area
$$(-\infty to p) = \int_{-\infty}^{p} \frac{1}{\sqrt{2\pi}} exp (-0.5 p') dp$$
 (A.2)

Figure A-4 gives the area under the Gaussian curve from -p to +p. This can be found from Eq. (A.3):

Area (-p tc +p) =
$$\int_{-p}^{+p} \frac{1}{\sqrt{2\pi}}$$

exp (-0.5 p²) dp (A.3)

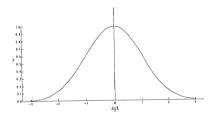


Figure A-1. The Gaussian distribution curve.

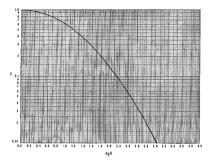


Figure A-2. Ordinate values of the Gaussian distribution.

ATMOSPHERIC DISPERSION ESTIMATES

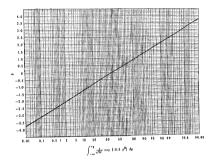


Figure A-3. Area under the Gaussian distribution curve from —- ∞ to p.

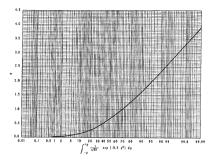


Figure A-4. Area under the Gaussian distribution curve between -p and +p.

Appendix 3: SOLUTIONS TO EXPONENTIALS

Expressions of the form $\exp [-0.5 \ A^{-}]$ where A is H/a, or y/σ_p frequently must be evaluated. Table A.1 gives B as a function of A where B - exp $[-0.5 \ A^{-}]$. The sign and fights to the right of the Eare to be considered as an exponent of 10. For example, if A is 3.51, B is given as 2.11E - 63 which means 2.11x 10⁻⁴

11100 11111 00444 1.101 2,83E 2,69E 2,68E 2,68E 1,56E 17E 238 536 536 965 928 598 278 9, 60E 7, 32E 7, 32E 13E 09E - 75E - 59E 11111 11111 22224 3.596 2.10E 8,715 8,916 9,916 65E 89E 38E -43E 385 796 916 9,916 1,95E 1,95E 1,95E 5,58E 6,58E 6,58E 12222 ~~~~ 4 4 4 10 10 50E 7 60E 7 73E 3,686 2,835 2,165 1,635 1,635 8.986 586 776 3.428 2.438 100000 04E 915 2 92E 682 2 985 2 92E 1,71E 1,20E 5,60E 89449 89449 89449 894 99E 99E 99E -----~~~~ 11111 00111 11179 222 111 8000 4, 52E 326 1.776 1.20E 9.70E 7.78E 875 916 916 226 576 9.26E 9.79E 9.54E 1,776 1,236 3,516 5,826 5,826 1,155 228 -----~~~~ **** 00111 77777 111111 3, 20E 895 895 695 695 8.60E 8.10E 7.55E 6.97E 5.766 5.766 5.766 5.766 5.766 5.766 5.766 5.766 5.766 5.766 01E 1.81E 1.22E 9.91E 6.32E 6.32E 8.876 2.995 2.285 1.725 1 835 1 285 845 845 845 745 826 206 786 786 ***** 22111 11111 11111 77999 10100 0.0E 61E 84E 1.255 1.016 8.166 9.176 976 976 976 976 976 976 7,236 7,236 3,785 3,785 1,906 1,396 9,186 6,282 346 22E SOLUTIONS TL The notation 2.1 77777 20222 100.000 100 - 100 2.650 2.650 1.555 1.27E 1.04E 8.32E 6.62E 2,07E 2,61E 2,61E 1,92E 1.028 7.468 3.438 3.918 1.38E 7.53E 6.53E 364.9 205 0.03 0.00E 0.02E 0.74E 0.47E 5.09E 364.4 140-1 11111 0.076 9.76 9.76 9.76 9.76 9.76 8.745 8.255 7.755 7.155 777 3.655 3.15E 2.2%E 1.915 1.31E 1.05E 5.31E 5.37E 4.19E 3.23E 2.47E 1.86E 1-05E 369.1 1.10E 305. 77222 1996 7.94E 3.43E 2.43E 1.52E 9.46E 8.785 7.775 7.775 7.205 9.40E * #15 4 245 3 705 3.205 241. 325 346. 1.335 1.085 A.705 A.946 20E 3.328 2.11E 1.48E 7.035 3.22E 2.15E 1.42E 9.25E 340.00 ~~~~ 11111 11199 91111 6.076 6.876 6.876 7.876 3.25E 2.36E 2.36E 100 C 4, 30E 3, 41E 2, 61E 1, 98E 1, 98E 111E 9.92E 9.09E 2,195 1,535 1,535 1,535 1,535 34E 48E 48E 25E 0.00 B 9.955 9.555 9.555 8.836 8.355 7.836 7.836 54E 54E 54E 0.00.00 89889 00000 89289 232.83 82889 4

ATMOSPHERIC DISPERSION ESTIMATES

~ 2

TO EXPONENTIALS B -- exp [--0.5A*1 2.16 E-1 metos 2.16 x 10^-1

able A-I

6°*0	2,376 -6 1,428 -6 8,386 -7 2,856 -7 2,856 -7	1.646 -7 9.326 -8 5.256 -8 2.936 -8	8-8+6 -9 4-706 -9 2-566 -9 1-366 -9 1-366 -9 1-316-10	1.91E-10 9.74E-11 4.92E-11 2.46E-11	1.226-01 5.955-12 2.885-12 1.965-12 6.565-13	3-096-13 1-446-13 6-656-14 3-046-14 1-376-14 1-376-14	1.195-15 5.185-16 2.235-16	4.00E-17 1.67E-17 6.89E-18 2.82E-18	1+146-14 +-586-19 1-826-19 1-146-20 2-768-20	1.076-20 4.086-21 1.546-21 5.766-22 2.136-22
9.06	2.49E -6 1.49E -6 8.84E -7 5.19E -7	1,736 -7 9,876 -8 5,576 -8 3,116 -8 3,116 -8	396 -9 2096 -9 6456 -9 626-10	04E-1 27E-1 63E-1	1.306-11 6.396-12 3.106-12 1.496-12 7.096-13	3-346-13 1-566-13 7-196-14 3-206-14 1-496-14 1-496-14 2-056-15 2-056-15	1+30E-15 5+64E+16 2+43E-16	4, 566-17 1, 826-17 7, 536-18 3, 056-18	L.256-18 5.028-19 1.996-19 7.848-20 3.058-20	1,186-20
0.07	2.626 -6 1.576 -6 9.326 -7 3.186 -7	1.836 -7 1.055 -7 5.005 -8 3.295 -8	9.986 -9 5.416 -9 2.916 -9 1.956 -9 8.136-10	2,195-10 1,125-10 5,646-11 2,826-11	L.40E-11 6.87E-12 3.34E-12 1.60E-12 7.64E-13	7.606-13 7.776-13 7.776-14 3.556-14 1.616-14 7.226-15 3.202-15	1-34	4.755-17 1.995-17 8.235-18 9.375-10	1.37E-18 5.50E-19 2.19E-19 8.61E-20 3.36E-20	1,306-20 4,956-21 1,676-21 7,026-22 2,606-22
90 • 0	2.765 -6 1.655 -6 7.75 -7 3.755 -7 3.755 -7	1.946 -7 1.116 -7 6.256 -8 3.496 -8	1,066 -8 5,766 -8 3,095 -0 1,055 -9 8,675 -9 8,675 -10	2,346-10 1,196-10 6,046-11 3,036-11	1,505-11 7,305-12 3,595-12 1,735-12 8,235-13	3,886-13 1,816-13 8,396-14 8,396-14 3,846-14 1,746-14 1,746-14 7,826-15 3,486-15	1,596-15 6,662-16 2,875-16 1,23£-16			1.45E-20 5.46E-21 2.07E-21 7.75E-22 2.88E-22
50°0	2.905 -6 1.745 -6 1.045 -6 6.095 -7 8.555 -7	2.056 -7 1.175 -7 5.622 -8 3.702 -8	1.136 -8 5.126 -9 3.296 -9 1.756 -9 9.256-10 9.256-10	2.506-10 1.286-10 6.476-11 3.256-11	1.616-11 7.925-12 9.866-12 1.865-12 8.876-12	4.196-13 1.966-14 9.076-14 4.166-14 1.896-14 1.896-14 8.486-15 8.486-15	1-262	5.66E-17 2.37E-17 9.83E-18 4.04E-18	1-64E-18 6-61E-19 2-63E-19 1-04E-19 4-06E-20	1+57E-20 6+01E-21 2+28E-21 8+55E-22 3+18E-22
9°°0	4-365 -6 4-36-1 6-36-1 6-36-0 1755 -6	2.176 -7 1.246 -7 7.016 -8 3.976 -8 2.196 -8	1,205 -8 5,515 -9 5,515 -9 1,875 -9 9,875 -9 9,875 -10	2.676-10 1.376-10 6.936-11	1,716-11 6,516-12 6,556-12 2,006-12 9,556-13	4,926-13 2,116-13 9,806-14 4,506-14 2,046-14 2,046-15 4,096-15	1.00E-15 7.97E-16 3.40E-16 1.66E-16	6.17E-17 2.59E-17 1.07E-17 4.41E-18	1,806-18 7,246-19 2,896-19 1,146-19 1,146-19 4,460-20	1, 73E-20 5,62E-21 2,51E-21 9,63E-22 5,51E-22
0.03	3,215 -6 1,936 -6 1,156 -6 0,786 -7 3,956 -7	2,296 -7 1,316 -7 1,426 -8 4,166 -8	1,276 -8 5,926 -9 3,736 -9 1,996 -9 1,096 -9	2.656-10 1.465-10 7.425-11	1.86E-11 9.14E-12 4.46E-12 2.15E-12 1.03E-12	*.87E-13 2,28E-13 1,06E-13 4,86E-14 2,21E-14 9,96E-15	1.96E-15 8.56E-16 5.70E-16	6.726-17 2.826-17 1.176-17 4.836-18	1.97E-18 7.93E-19 3.17E-19 1.25E-19 4.90E-20	1,90E-20 7,29E-21 2,77E-21 1,04E-21 3,48E-22
0,02	3.376 -0 2.096 -6 1.216 -6 7.156 -7	2.625 -7 1.395 -7 7.865 -7 7.615 -8	9- 321-1 9- 376-1 9- 376-1 1-120-0	9 056-10 1 556-10 7 956-11	1,995-11 9,815-12 4,795-12 2,326-12 2,326-12 1,116-12	5.255-13 2.465-13 1.145-13 5.265-14 2.395-14 2.395-14 1.085-14	2.13E-15 9.30E-15 4.03E-16	7.336-17 3.096-17 1.296-17		2.096-20 8.026-21 3.096-21 1.156-21 1.156-21
10*0	3-558 -0 2-1488 -0 1-2888 -0 7-5948 -0 1-2888 -1	2.56E -7 1.47E -7 3.32E -8	2,256 -9 2,256 -9 2,256 -9 1,206 -9	3.256-10 1.676-10 8.506-11	2,146-11 1,056-11 5,156-12 2,496-12 2,496-12	5.666-13 2.666-13 5.666-13 5.696-15 2.596-14 2.596-14	2.316-15	1.995-17 3.365-17 1.405-17 5.776-18	2.366-19 9.526-19 3.816-19 1.516-19 1.516-19 5.926-20	2,30E-20 8,88E-61 3,36E-61 3,36E-61 1,27E-21 1,27E-21
0.00	3.75E -6 2.25E -6 1.35E -6		2,76E -3 1,52E -8 8,32E -9 2,41E -9 2,41E -9 1,23E -9	6.696-10 3.496-10 1.796-10 9.106-11	2.296-11 1.196-11 5.546-12 2.686-12 1.296-12	6.106-13 2.876-13 1.946-13 6.1946-13 5.806-14 7.276-14	2,515-15	2.0%E-16 8.710-17 3.670-17 1.510-17 1.510-17	4.58E-18 1.04E-18 4.18E-19 1.66E-19 6.50E-20	2.536-20 9.726-21 9.776-21 1.406-21
	001220		8.93 9.93 9.93 9.93 9.93 9.93 9.93 9.93	992 993 993 993 993 993 993 993 993 993	00111	4-50 4-60 8-00 8-00 8-00 8-00 8-00 8-00 8-00 8	8.30 8.30 8.40	8-90 9-90 9-90 9-90 9-90 9-90 9-90 9-90	00100	000000000000000000000000000000000000000

Table A-1 (continued) SOLUTIONS TO EXPONENTIALS

ppendix 3

Appendix 4: CONSTANTS, CONVERSION

EQUATIONS, CONVERSION TABLES

Constants

$$\begin{split} \mathbf{e} &= 2.7183 - \frac{1}{\mathbf{e}} = -0.3679 \\ &= -3.1416 - \frac{1}{\tau} = -0.3183 \\ 2\pi &= 6.2832 - \frac{1}{2\pi} = -0.1682 \\ &\sqrt{2\pi} = 2.5066 - \frac{1}{\sqrt{2\pi}} = -0.3989 \\ &\frac{2}{\sqrt{2\pi}} = 15.75 - \frac{2}{\sqrt{2\pi}} = -0.7979 \\ &(2\pi)^{1/2} = 15.75 - \frac{2}{\sqrt{2\pi}} = 0.7979 \end{split}$$

Conversion Equations and Tables

 $\begin{array}{l} T(^{\circ}C) = 5/9 \ (T(^{\circ}F) \ -32) \\ T(^{\circ}K) = T(^{\circ}C) \ +273.16 \\ T(^{\circ}F) = (9/5 \ T(^{\circ}C) \) \ +32 \end{array}$

CONVERSION FACTORS - VELOCITY	- VELOCITY						
DESTRED UNITS NETERS PER SEC GIVEN UNITS	METERS PER SEC	FT PER SEC	FT PER MIN	KM PER HR	HI (STAT) PER HR	KNOTS	NI (STAT) PER DAY
HETERS	E 00	3.2808	1,9685	3.6000	2,2369	L+9425	5.3686
PER SEC		E 00	E 02	E 00	E 00	E 00	E 01
FT PER SEC	3.0480	1.0000	6.0000	1,0973	6.8182	5.9209	1,6364
	E=01	E 00	E 01	E 00	E-01	E-01	E 01
FT	5.0800	1.6667	1,0000	1.8288	1.1364	9.8681	2,7273
PER MIN	E=03	E-02	E 00	E-02	E-02	E=03	E=01
KN	2.7778	9.1134	5.4681	1.0000	6.2137	E-01	1,4913
PER HR	E-01	E-01	E 01	E 00	E-01	5*3959	E 01
MI (STAT)	4.4704	1.4667	8.8000	1.6093	L.0000	8.6839	2.4000
PER HR	E-01	E 00	E 01	E 00		E-01	E 01
KNOTS	5,1479	1.6889	1,0134	1,8532	1.1516	1,0000	2,7637
	E-D1	E 00	E 02	E 00	E 00	E 00	E 01
MI(STAT)	1,8627	6.1111	3.6667	6.7056	4.1667	3.6183	1+0000
PER DAY	E-02	E-02	E 00	E-02	E-02	E-02	E 00
TO CONVERT A VALUE P	FRON A GIVEN	A UNIT TO A	DESIRED UNI	T. MULTIPLY	THE GIVEN	VALUE BY TH	TO CONVERT A VALUE FROM A GIVEN UNIT TO A DESIRED UNIT, MULTIPLY THE GIVEN VALUE BY THE FACTOR DPPOSITE THE

GIVEN UNITS TO CONVERT A VALUE FROM A GIVEN UNIT TO A UESIRED UNIT, MULITPLY THE GIVEN AND BENEATH THE DESIRED UNIT. NOTE THAT E-XX MEANS 10 TO THE +XX POWER.

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ATMOSPHERIC DISPERSION ESTIMA

	٨Y							1.				
	TONS PER DAY		9.5240 E=02	1,5873 E-03	2,6455 E=02	1,1023 E=03	7,2000 E=01	1,2000 E-02	5,0000 E-04	2,4000 E 01	1,0000 E 00	,
	PER HOUR		5.9683 E-03	6+6139 E=05	1,1023 E-03	4-,5930 E-05	3+0000 E+02	5+0000 E=04	2+0833 E=05	1,0000 E 00	4,1567 E-02	
	LBS PER DAY		E 02	3.1747 E 00	5,2911 E 01	2+2046 E 00	1.4400 E 03	2.4000 E 01	1.0000 E 00	4.8000 E 04	2.0000 E 03	A DESTRICT MULTIPLY THE GIVEN VALUE AN THE EACTOR SOCIAL MULTIPLY AND
	PER HOUR		7.9366 E 00	1,3228 E-01	2.2046 E 00	9.1859 E-02	6*0000 6 01	1,0000 E 00	4.1667 E-02	2.0000 E 03	8.3333 E 01	A THE STATE
	LBS. PER MIN		1.3228 E-01	2,2046 E-03	3.6744 E-02	1,5310 E-03	1.0000 E 00	1,6667 E-02	6,9444 E-04	3,3333 E 01	1,3889 E 00	Manual and a
	KG PER DAY		8.6400 E 01	1.4400 E 00	2,4000 E 01	1.0000 E 00	6,5317 E 02	1.0886 E 01	4.5399 E-01	2,1772 E 04	9.0718 E 02	T. MILL TTOL
	PER HOUR		E 00	5,0000 E-02	L.0000 E 00	4,1667 E-02	2,7216 E 01	4,5359 E-01	1.8900 E-02	9.0718 E 02	3.7799 E 01	THE OWNER
RATES	GRAMS) PER MIN		6.0000 E 01	1,0000 € 00	1,6667 E 01	6,9444 E=01	4.5359 E 02	7,5599 E 00	3.1499 E=01	1.5120 E 04	642999 E 02	
CONVERSION FACTORS - EMISSION RATES			E 00 0	1,6667 E-02	2,7778 J E-01	1,1574 0 E-02	7.5599 4	1,2600 E-01	5,2499 E-03	2,5200 E 02	E 01	and a second second
EACTORS -	DESTRED UNITS GRAMS PER SEC	s	-									
CDNVERSION	DESTR	GIVEN UNITS	GRAMS PER SEC	GRAMS PER MIN	K6 PER HOUR	KG PER DAY	LBS PER MIN	LBS PER HOUR	LBS PER DAY	TDN5 PER HDUR	TONS PER DAY	and others a set

endix 4

CONVERSION FACTORS - LENGTH	- LENGTH								
DESIRED UNITS METER	5 METER	5	MICRON	KILOMETER	LNCH	FOOT	YARD	MILE(STAT) MILE(WAUT)	HILE (NAUT)
GIVEN UNITS									
METER	1,0000	1,0000	1.0000	1.0000	3,9370	3.2808	1,0936	6,2137	5,3959
	E 00	E 02	E 06	E-03	E 01	E 00	E 00	E= '4	E=04
ð	1.0000	1.0000	1+0000	1.0000	3,9370	3,2808	1.0936	6.2137	5,3939
	E-02	E 00	E 04	E-05	E-D1	E=02	E=02	E=06	E=06
MICRON	1+0000	1,0000	1+0000	1.0000	3,9370	3.2808	1+0936	6,2137	5,3959
	E-06	E-04	E 00	E=09	E-05	E~06	E-06	E=10	E-10
KILONETER	1,0000	1.0000	1,0000	1,0000	3,9370	3+2808	1.0936	6-2137	5,3959
	E 03	E 05	E 09	E 00	E 04	E 03	E 03	E-01	E=01
INCH	2.5400	2.5400	2.5400	2.5400	1.0000	8.3333	2.7778	1,5783	1.3706
	E-02	E 00	E 04	E=05	E 00	E=02	E-02	E=05	E-05
FOOT	3.0480	3.0480	3+0480	3.0480	1.2000	1,0000	3,3333	1,8939	1.6447
	E-01	E 01	E 05	E-04	E 01	E 00	E=01	E=04	E-04
YARD	9,1440	9.1440	9.1440	9.1440	3.6000	3,0000	1.0000	5.6818	4,9340
	E-01	E ol	E D5	E=04	E 01	E 00	E 00	E=04	E-D4
MILE(STAT)	1.6093	1.6093	1.6093	1.6093	6,3360	5.2800	1.7400	1,0000	8.4839
	E 03	E 05	E 09	E 00	E 04	E 03	E 03	E 00	E=01
HILE (NAUT)	1,8532	1.8532	1.8532	1.8532	7,2962	6+0802	2,0267	1,1516	1,0000
	E 03	E 05	E 09	E D0	E 04	E 03	E 03	E 00	E 00
TO CONVERT A VALUE FROM A GIVEN UNIT And Beneath the desired unit. Note	FROM A GIVEN IRED UNIT.	UNIT TO A NOTE THAT	DESTRED UNI	10 TO THE -	THE GIVEN XX POWER.	VALUE BY 1	HE FACTOR O	TO A DESIGED UNIT, MULTIOLY THE GIVEN VALUE BY THE FACTOR OPPOSITE THE GIVEN UNITS THAT E-XX MEANS ID TO THE -XX POWER.	GIVEN UNITS

CONVERSION FACTORS - LENGTH

ATMOSPHERIC DISPERSION ESTIMATE

CONVERSION FACTORS - AREA	RS - AREA								
DESIREO UNI	DESIRED UNITS SO METER	SQ KW	SD CH	50 INCH	50 F001	SQ YARD	ACRE	SC STAT	SO NAUT MILE
GIVEN UNITS									
SD NETER	1,0000 E 00	1,0000 E-06	L 0000	E 03	E 01	E 00	E=04	E-07	2.9116 E-07
SO KM	1,0000	1.0000	1,0000	1.5500	1.0764	1,1960	2.4710	\$,8610	2,9116
	E 06	E 00	E 10	E 09	E 07	E 06	E 02	E=01	E=01
Så CH	1,0000	1,0000	1,0000	1.5500	1,0764	1.1960	2.4710	3,8610	2,9116
	E-04	E-10	E 00	E-01	E-03	E-04	E-08	E-11	E=11
SO INCH	6.4516	6,4516	6+4516	1.0000	6+9444	7.7160	1.5942	2,4910	1,8785
	E-04	E-10	E 00	E 00	E-03	E.04	E-07	E=10	E-10
So FOOT	0,2903	9.2903	9, 2903	1.4400	1.0000	1.1111	2.2957	3.5870	2.7050
	E-02	E-08	E 02	E 02	E 00	E-01	E-05	E.08	E-08
SD YARD	8.3613 E=01	8.3613 E-07	6.3613 E 03	1,2960 E 03	9*0000	1.0000 E 00	2.0661 E-04	3,2283 E=07	2,4345 E-07
ACRE	4,0469	4.0460	4.0469	6.2726	4.3560	4.8400	1.0000	1.5625	1,1783
	E 03	E-03	E 07	E 06	E 04	E 03	E 00	E-03	E-03
SD STAT	2.5900	2.5900	2,5900	4.0145	2,7875	3,0976	6.4000	1,0000	7.5411
WILE	E 06	E 00	E 10	E 09	E 07	E 06	E 02	E 00	E+01
50 NAUT	3.4345	54545	3,4345	5,3235	3.6969	4,1076	8,4869	1,3261	L, 0000
MILE	E 06	5*4345	E 10	E 09	E 07	E 06	E 02	E 00	E 00
TO CONVERT A VALUE FROM A GIVEN L AND BENEATH THE DESIRED UNIT.	UE FROM A GIN DESIRED UNIT.	EN UNIT TO NOTE TH	A DESIRED AT E-XX MEA	UNIT, MULTIF NS 10 TO THE	PLY THE GIVE	EN VALUE BY	THE FACTOR	OPPOSITE TI	UNIT TO A DESIRED UNIT, MULTIPLY THE GLVEN VALUE BY THE FACTOR OPPOSITE THE SIVEN UNIT NOTE THAT E-XX WEARS 10 TO THE -XX PONER.

Appendix 4

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CONVERSION FACTORS - VOLUME	3 - VOLUME								
DESTRED UNITS	S CU METER	LI TEV	CO INCH	CU FODT	CU STAT	CU NAL	50	U 5 DUART	N 2 GALLON
GIVEN UNITS					אנורב	AILE .	DUKCE		
cu METER	1,0001	9.9997	6,1023	3,5314	2,3991	1.5711	3.3814	1,0567	2,6417
	F n0	E 04	E 04	E 01	E-10	E-10	E 04	E-03	E 02
LITER	1.0000	00 3	6,1025	3.5315	2,3992	1.5711	3,3815	1,0567	2.6418
	E-03	1*unuo	E 01	E-n2	E-13	E-13	E 01	E-06	E-01
CU INCH	1,6 ⁹⁸⁷	1.63#7	1.0000	5.7470	3,9315	2,5746	5.5412	1.7316	4.3290
	5-05	E-02	F 00	E-04	E-15	E-15	E-01	E-08	E-03
cu Foot	2,8117 E-02	2,9316 E 01	1.7280 E 03	1,0000	6.7936 E-12	4,4488 E-12	9.5751 E 02	2.9922 E-05	7.4805 E 00
CU STAT	*,1684	4,1641	2.5436	1,4720	1,0000	64966	1.4094	4.4045	1,1011
MTLE	E 09	E 17	E 14	E 11	E 00	E-01	E 14	E 06	E 12
CU MAUT	6, 3650	6.3649	3,8542	2,2478	1,5270	1,0000	2,1523	6.7259	1,6815
MILE	E 79	E 12	E 14	E 11	E 00	E 00	E 14	£ 06	E 12
U S FLUID	2.9574	2.9573	1,8047	1,0444	7.0950	4,6462	1,0000	3,1250	7.8125
	F-95	E-02	E 90	E-03	E-15	E-15	E 00	E-08	E-03
U S DUART	9.4635	9.4633	5.7750	3,3420	2,2704	1.4868	3.2000	1,0000	2,5000
	E 02	E 05	E 07	E 04	E-07	E-07	£ 07	E 00	E 05
n S GALLON	3.7854	3.7853	2.3100	1.3368	9,0817	5,9472	1,2800	4,000.0	1,0000
	E-03	E 00	E 02	E-01	E-13	E-13	E 02	E-06	E 00
TO COWVERT A VALUE REAM A GIVEN UNIT TO A DESIRED UNIT, MULTIONY THE GIVEN VALUE OY THE FACTOR OPODSITE THE GIVEN UNITS AND BEERTHA THE DESIRED UNIT, ANTE THAT EXX TERVELOD TO THE AXY COURS,	FRON A GIVE SIRED UNIT.	N UNIT TO A	A DESIRED U	NIT. HULTIP	LY THE GIVE	VALUE OY	THE FACTOR 0	PPOSITE THE	E GIVEN UNITS

ATMOSPHERIC DISPERSION ESTIM

CONVERSION FACTORS - MASS DESIRED UNITS GRAM	- MASS GRAM	MICROSRAM	KILDGRAM	METRIC TON	METRIC TON SHORT TON	LONG TON	GRAIN	OUNCE (AVDP)	(90/A)
GIVEN UNITS	1,0000	1,0000	1,0000	1,0000	1.1023	9,8421	1.5432	5274	2,2046
GRAM	E 00	E 06	E-03	E=06	E-06	E-07	E 01	€=02	E=03
M1 CROGRAM	1,0000	1,0000	1,0000	1,0000	1,1023	9,8421	1.5432	5,5274	2,2046
	1,0000	E 00	E-09	E-12	E-12	E-13	E-05	E=08	E-09
KILDGRAM	E 03	1,0000	1,0000	1.0000	1,1023	9,8421	1 ,5432	3,5274	2,2046
	E 03	E 09	E 00	E-03	E-03	E=04	E 04	€ 01	E 00
NETRIC TON	1,0000	1,0000	1,0000	1.0000	1,1023	9,8421	1.5432	5,5274	2,2046
	E 06	E 12	E 03	E 00	E 00	E=01	E 07	E 04	E 03
SHORT TON	9,0718	940718	9,0718	9.0718	1,0000	6,9286	1.4000	3,2000	2,0000
	E 05	E 11	E 02	E=01	E 00	E=01	E 07	E 04	E 03
LONG TON	1,016 ⁰	1,0160	1.0160	1,0160	1,1200	1.0000	1,5680	3 , 5840	2,2400
	E 06	E 12	E 03	E 00	E 00	E 00	E 07	E 04	E 03
GRAIN	6.4799	6.4799	6.4799	6.4799	7,1428	6+3775	1.0000	2,2857	1.4286
	E-02	E D4	E-05	E-08	E+05	E-08	E 00	E=03	E-04
OUNCE	2,8349	2.8349	2,8349	2,8349	3.1250	2.7902	4.3750	1, 0000	005+00
(AVDP)	E 01	E 07	E-02	E-05	E-05	E-05	E 02		E+02
LB (AVDP)	4,5359	4.5359	4.5359	4.5359	5,0000	4,4643	7.0000	10 3	1,0000
	E 02	E 08	E-01	E-04	E-04	E-04	E 03	1 6000	E 00
	TAL A MARK	IN UNIT TO A	A DESTRED IN	ALT. MILTER	Y THE GLUEN	VALUE BY	THE FACTOR	OPPORTE THE	

TO COMPERT A MALLE FROM A GIVEN UNIT TO A DESIRED UNIT, MULTPAY THE GIVEN WALLE BY THE FACTOR OPPOSITE THE GIVEN UNITS AND BENEATH THE DESIRED UNIT. MOTE THAT E-XX MEANS 10 TO THE -XX POMER.

idix 4

s sec		_	_						
CU CH	1,0000	2,7778	1,0000	1,6667	2,7779	2,8317	4.7195	7,8658	1,0000
PER	E 06	E 02	E 03	E 01	E-01	E 04	E 02	E 00	E 00
NIN PER HR	1.2713	5314	1,2714	2,1189	5315	3,6000	6,0000	1,0000	1,2713
	E 05	5 01	E 02	E 00	E-02	E 03	E 01	E 00	E-01
CU FT	2.1189	5*8857	2+1189	3.5315	5.8859	6*0000	1,0000	1+6667	2.1189
SEC PER	E 03	E-01	E 00	E-02	E-04	E 01	E 00	E+02	E=03
CU FT	3,5314	9,8096	3+5315	5,8859	9.8098	1,0000	1.6667	2.7778	3.5314
	E 01	E-03	E-02	E=04	E-06	E 00	E-02	E-04	E=05
LITER	3.5999	9 4 9997	3.6000	6,0000	1,0000	1,0194	1.6990	2,8316	3*5999
PER HR	E 06	E 02	E 03	6,0000	E 00	E 05	E 03		E 00
LITER	5.9998	1.6666	6.0000	1,000	1.6667	L_699D	2.8316	4.7194	5,9998
PER MIN	E 04	E 01	E 01	E 00	E=02	E 03	E 01	E-01	E=02
LITER	9.9997	2.7777	1.0000	1.6667	2,7778	2,8316	4.7194	7,8656	9,9997
PER SEC	E 02	E-01	E 00	E+02	E+04	E 01	E-01	E-03	E-04
CU METER	3.6000	1.0000	3.6001	6.0002	1,0000	1,0194	1.699D	2,8317	3.6000
PER HR	E 03	E 00	E 00	E-02	E-03	E 02	E 00	E-02	E-03
DESIRED UNITS CU 4ETER	1,0000	2.7778	1+0000	1,6667	2.7779	2,6317	4.7195	7.8658	1.0000
I UNITS PER 5EC	E 00	E+04	E-03	E+05	E-07	E-02	E-04	E-D6	E-06
DESIRED UN	CU NETER	CU METER	LITER	LITER	LITER	cu FT	CÚ FT	CU FT	cu cw
GIVEN UNITS	PER SEC	PER HR	PER SEC	PER'NIN	PER HR	PER sec	PER MIN	PER HR	Per sec

TO CONVERT A VALUE FROM A GIVEN UNIT TO A DESIRED UNIT, MULTIPLY THE GIVEN VALUE BY THE FACTOR OPPOSITE THE GIVEN UNITS AND BENEATH THE DESIRED UNIT. NOTE THAT E-XX MEANS IO TO THE -XX PONDE.

ATMOSPHERIC DISPERSION ESTIMATES

CONVERSION FACTORS - FLOM

CONVERSION FACTORS - CONCENTRATION. DENSITY

GRAM PER LIS PER CU FT CU METER 2,2072 E 00 8,5314 E 01 7.7855 E-02 2.2046 E-03 6-03 E-03 E 0000 , 2046 E=06 . 2046 E=09 1,2046 E-06 E 01 L, 2844 E 01 6.8317 E-02 ., 8317 E=05 .. 8317 E-08 .8316 E-05 £-02 £ 02 E 000 CG FT OUNCE PER LB PER CU FT CU 5.2427 E.08 E-04 2,2046 E=03 2.8317 E-02 6.2428 E-05 6.2428 E-08 -2428 E-11 6.2500 E-02 1,0000 E-03 E 000 . 6000 3.5274 E-02 6-01 E-01 9+9885 E-04 5-07 E-07 , 9885 E-10 E-01 MICROGRAM MICROGRAM GRAIN PER PER CU M PER LITER CU FT r,0000 E 01 -3700 E-01 •.3700 E-07 4,3699 E-04 1,0000 4,3750 E 02 L,9822 E 02 4, 3700 E=04 3.5315 E 04 E 05 E 03 E 00 L.0000 E 00 2,2884 E 03 1,0012 1,6019 E 07 E 10 8.5314 E 07 6,5359 E 08 1,0000 E 06 . 0000 E 03 1.0000 9,9997 E 02 2,2883 E 06 1,0011 CU VETER MG PER • 5359 E 05 5,5314 E 04 1.0000 E 03 0000 . 0000 E-03 0.9997 E=01 2.2883 E 03 1,0011 E 06 1.6018 E 07 DESIRED UNITS GRAW PER CU HETER 8,5314 E 01 4,5359 E 02 E 00 1100,1 1,6018 E 04 • 0000 1.0000 E-06 -047 E-04 STVEN UNITS OUNCE PER GRAN PER CU FT NICROGRAM PER LITER GRAIN PER CU FT CU METER SRAM PER CU METER CU NETER PER CU N LB PER CU FT NTCROGRAM MG PER LB PER

O CONCERT A VALUE FROM A GIVEN UNIT TO A DESIGED UNIT, WULTIPLY THE GIVEN VALUE BY THE FACTOR OPPOSITE THE GIVEN UNITS And deficient the desired unit. Mote that E-XX Means 10 to the -XX POMEA.

Appendix 4

MG PER SO IN PER NO 6-01 E-01 5.4516 E=04 5,4516 E 00 .2598 E-01 E 02 .2313 E.02 5.9444 E 00 L.0000 DESIRED UNITS GN PER SO, KG PER SO, MG PER SO, DO PER SO, D2 PER SO, LNITS GN PER SO, M N PER NO, KN PER NO, KN PER NO, MI PER NO, FT PER NO, ACRE PERNO, FT PER NO 9.2903 E-02 •,2903 E=05 •. 2903 E-01 5.2541 E-02 E 01 .0413 E-02 • 0000 1044 6.9216 E 00 5.9218 E-03 8.9218 E 01 8.1250 E 00 E 03 1.0000 E 00 9.6033 E 01 1,3829 E 01 6-03 E-03 5.2771 E-06 5.2771 E-02 L.1478 E-03 8.6731 E-04 3.5274 E-02 5,0795 E-03 (SHORT TON .STAT. MILE) E 00 E-03 E 01 1, 0000 5*7120 E 02 5.2000 E-01 6,0731 E 01 ****** 1,0000 E=01 0000° 3.5026 E-02 8.0515 E 01 ..1208 E-02 *0764 E 00 -0000 E-04 E-01 E 03 E 000 3.5024 E 02 6,0515 E 05 .0764 E 04 1,0000 E 02 1.5500 E 03 CONVERSION FACTORS - DEPOSITION RATE 1,0000 E 00 1,0000 E-03 1,0000 I 3.5026 E-01 3,0515 E 02 1.1208 E-01 1.0764 E 01 1.5500 E 000 STVEN UNITS GH PER SO M PER NO MG PER SO CM PER HO LB PER ACRE PERMO MG PER SO IN PER MO K& PER SO KN PER HO MI PER NO DZ PER 50 FT PER MO EN PER 50 FT PER MO

THE FACTOR OPPOSITE THE GIVEN UNIT: TO CONVERT A VALUE FROM A GIVEN UNIT TO A DESIRED UNIT, MULTIPLY THE GIVEN VALUE BY AND BENEATH THE DESIRED UNIT. NOTE THAT E-XX MEANS 10 TO THE -XX POMER.

ATMOSPHERIC DISPERSION ESTIMAT

IM MERCURY IN NERCURY E-02 E 01 E 00 . 9370 E-02 E 01 E 01 E=05 1,0000 E 00 -9006 E=04 r, 3556 E 02 5.1715 E 01 E 000 E 01 . 5006 E-01 1.5006 E 02 E 02 ATNOSPHERE DYNES KG LBS | PER SO CM PER SO CM PER SO IN L+504 E-02 . 4504 E 01 E 01 E-05 1,4223 E 01 L,0000 L. 9337 E-02 4.9115 E-01 L.0197 E-03 L.0332 E 00 L.0197 E-06 0000 .0307 E-02 ...3595 E-03 3,4532 E-02 e 00 3 6.3066 L.3332 E 05 3,3864 E 04 E 03 E 06 1.0133 E 06 E 000 9,8692 E-04 5692 E-01 1.0000 E 00 9.8692 E-07 . 6784 E=01 6.8046 E-02 L+3158 E-03 8,3421 E-02 E 00 .8066 E-01 6.8947 E-02 ..3332 E-03 3.3864 E-02 -0000 • 0000 L.0000 848 CONVERSION FACTORS - PRESSURE DESIRED UNITS MILLIBAR 8066 E 02 5,8947 E 01 • 3332 E 00 5,3864 E 01 E 0000 E 03 E 03 . 0000 GIVEN UNITS DYNES PER SD CH ATNOSPHERE KG PER SO CH BS PER SO IN AN NERCURY IN MERCURY MILLIBAR AR.

O CONVERT A VALUE FROM A GIVEN UNIT TO A DÉSPRÉD UNIT, MULTIPLY THE GIVEN VALUE BY THE FACTOR OPPOSITE THE GIVEN UNITS AND DEGLETAT THE DESTRED UNIT. NOTE THAT E-XX MEANS 10 TO THE +XX POWER.

Appendix 4

DESIRED UNITS	S SECOND	MINUTE	ноик	NEEK	MONTH (28)	MONTH (30)	(18) HINOW (YEAR (365)	YEAR (36)
GIVEN UNITS									
AECOND	1,0000	6,0000	3,6000	\$0 3	2,4192	2,5920	2,6784	3,1536	3,1622
	E 00	E 01	E 03	E 0480	E 06	E 06	E 06	E 07	E 07
MINUTE	1.6667	1.0000	6,0000	1,0080	4.0320	4,3200	4,4640	5,2560	5, 2704
	E-02	E 00	E 01	E 04	E 04	E 04	E 04	E 05	E 05
HOUR	2,7778	1.6667	1,0000	1.6800	6,7200	7,2000	7,4400	8,7600	8,7840
	E-04	E-02	E 00	E 02	E 02	E 02	E 02	E 03	E 03
VEEK	1,6534	9.9206	5,9524	1,0000	4*0000	4.2857	4.4286	5,2143	5,2286
	E+06	E=05	E-03	E 00	E 00	E 00	E 00	E 01	E 01
MDNTH (28)	4.1336	2.4802	1.4881	2.5000	1.0000	1,0714	1+1071	1,3036	1,3071
	E-07	E-05	E=03	E-01	E 00	E 00	E 00	E 01	E 01
MONTH (30)	3.8580	2.3148	1.3889	2.3333	9.3333	1+0000	1+0333	1,2167	1,2200
	E-07	E-05	E-03	E-01	E=01	E 00	E 00	E 01	E 01

(366) Ν. TO CONVERT A VALUE FROM A GIVEN UNIT TO A DESTRED UNIT, MILTIPLY THE GIVEN VALUE BY THE FACTOR OPPOSITE THE GIVEN UNITS AND BENEATH THE DESIRED UNIT. NOTE THAT E-XX MEANS IO TO THE -XX POMER.

8.4699 E-02 8.4932 E-02

8.1967 E=02 8,2192 E=02

1,1806 E 01 L.0027 E 00 L,0000

1,1774 E 01 E 000 9,9727 E=01

1,0000

6774 .

9,0323 E-01 7.6712 E-02 7.6503 E-02

2.2581 E-01 1.9178 E-02 1.9126 E-02

..3441 E-03 1.1416 E-04 1.1384 E-04

2+2401 E-05 L-9026 E-06

3, 7336 E-07 3.1710 E-08 3.1623 E-08

MONTH (31) YEAR (365) YEAR (366)

ATMOSPHERIC DISPERSION ESTIMATES

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CONVERSION FACTORS - TIME

5) ELECT. HORSEPOWER	1,3407 E+03	1,3407 E 00	1,3407 E 03	5,6145 E-03	2,3581 E-02	3,9301	1,3405 E-D3	1,3405	1,0000	2
JOULES ABS WATT (ABS) PER SEC	1.0002 E 00	1,0002 E 03	1,0002 E 06	4.1884 E 00	1,7591 E 01	2.9319 E-D1	1,0000 E 00	1+0000 E 00	7.4600 E 02	
	1,0002 E 00	1.0002 E 03	1,0002 E 06	*.1884 E 00	1,7591 E 01	2.9319 E-01	1,0000 E 00	1.0000 E 00	7.4600 E 02	
41N BEU	5.4114 E 00	4114°5	5.4114 E 06	1.4286 E 01	6,0000 E 01	1,0000 E 00	3.4108 E 00	3.4108 E 00	2,5444 E 03	N VALUE BV
etu PER 41N	5,6857 E-02	2.6857 E 01	>. 6857 E 04	2,3310 E-01	1,0000 E 00	L. 6667 E-02	>,6846 E-02	5,6846 E-02	10 3 E 01	THE GIVE
CAL (141)	2.3480 E-01	2. 1430 E 12	2, 3430 E 05	1. Diton E 05	4,2100 £ 30	7, 9000 5-92	5/3812 5/10-3	2,3875 E-01	1,7411 4 E 02	T. MULTIPLY
TEGOMATT (TWT)	1.0000 E-06	1,0000 F-03	1.0009	4,1476 8-06	1.7584 E-05	2.9313 E-07	9,9981 E-07	9.9981 E-07	7.4536 E-04	DESTREP UNI
Z1LDHATT (111)	1,0000 6-03	1,0000 E 00	1,0000 E 05	4.1876 E-03	1,7548 E-02	2.0313 E-04	е.9941 Е-04	ъс-3 Тябь°ь	7.45×6 E-01	A OT LIVU N
UNITS WATT	0000°1	1, unon	1,0000 E 06	4*1876 F 00	1,7588 F 01	2,9313 E-01	9-9481 E-01	9.9981 E-01	7.4586 E n2	UF FROM A GIVE
DFSIRFU UNITS AATT GIVEN IMITS	WATT (INT)	KIN DWATT (INT)	WESAWATT (INT)	CAL LINT) PER SEC	87U PER '1IN	BTU PER ⊣R	JOULES ABS PER SEC	WATT CATS!	ELECT. HORSEPOWER	TO CONVERT A VALUE FROM A GIVEN INTEL TO A DESTRED UNIT, MULTIPLY THE GIVEN VALUE BY TWE FILTER.

Appendix 4

CONVERSION FACTORS - ENERGY. WORK

TO CONVERT A VALUE FROM A GIVEN UNIT TO A DESIRED UNIT, MULTIPLY THE GIVEN VALUE BY THE FACTOR OPPOSITE THE GIVEN UNIT AND BENEATH THE DESIRED UNIT. NOTE THAT E-XX WEANS ID TO THE -XX PONER.

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ATMOSPHERIC DISPERSION ESTIMATES

CONVERSION FACTORS - ENERGY PER UNIT AREA	- EVERGY	PER UNIT AREA			
DESTRED UNITS LANGLEY	LANGLEY	CAL (15) PER 50 CH	CAL (15) BTU INT KW-HR PER 50 CH PER 50 M	INT KW-HR PER SO M	ABS JOULES PER SO CM
GIVEN UNITS					
LANGLEY	1,0000	1,0000 E 00	3,6855 E 00	1,1624 E-02	4.1855 E 00
CAL (15)	1,0000 E 00	1,0000 E 00	3,6855 E 00	1,1624 E-02	4.1855 E 00
	2,7133	2,7133	1,0000	3,1540	1,1357 F 00
PER So FT	E-01 8,6029	E=01 8,6029	3.1706	1,0000	3,6007
PER SO M	E 01 2,3892	E 01 2,3892 F_01	E 02 8,8054 E=01	2,7772 2,7772 E-03	1.0000 E 00
		ATT	010-020	T. MILTIN	Y THE GIVEN

O CONVERT A MALUE FROM A GIVEN UNIT TO A DESISEO UNIT, MULTPLY THE GIVEN VALUE BY THE FACTOR OPPOSITE THE GIVEN UNITS AND BENEFIN THE DESIRED UNIT. NOTE THAT E-XX MEANS 10 TO THE -XX POMEA.

	NATT R SD CH	4.1855 E-04	6.9758 E-02	6.9758 E-02	4,8443 E-05	.+8928 E-02	1.3144 E-05	E 00	
	SQ A65 DAY PE	34	6.9 E	6"9 6"1	4 8 1	37	34	3°	
	STU PER	3,1843 E 01	5,3071 E 03	5,3071 E 03	3.6855 E 00	1,4400 E 03	1.0000 E 00	7.6079 E 04	
	BTU PER SO BTU PER SO ABS WATT FT PER MIN FT PER DAY PER SO CH	2+2113 E-02	3.6855 E 00	3,6855 E 00	2.5594 E=03	1,0000 E 00	6.9445 E-04	5,2633 E 01	
(CAL ARE 12 DEG)	CAL PER 50 CM PER 0AY	8.6400 E 00	1.4400 E 03	1.4400 E 03	1,0000 E 00	3.9072 E 02	2,7133 E=01	2.0643 E 04	
CAL ARE	ANGLEY	6-03 E-03	1.0000 E 00	1.0000 E 00	6.9444 E-04	2.7133 E-01	1,8843 E-04	E 01	
CALL AKEN	CAL PER SQ LANGLEY CAL PER 50 CM PER NIN PER NIN CM PER DAV	6-0000 E-03	E 0000	1+0000 E 00	6-9444 6 E-04	2,7133 2 E-01	1.8843 E-04	1,4335 1 E 01	
HONE FIND HEL HERDE - DEDITEL HOTOHANDO	DESIREO UNITS CAL PER 50 M PER SEC UNITS	1,0000 E 00	1.6667 E 02	1.6667 E 02	1,1574 E-01	4.5222 .	3.1404 E-02	2,3892 E 03	AND A REAL
	EO UNITS (S	-	-	-	-	4		8	
NOTON AND A	DESTRE	CAL PER SO H PER SEC	CAL PER 50 CM PER NIN	LANGLEY	CAL PER SO CM PER DAY	BTU PER SQ FT PER MIN	BTU PER SO FT PER DAY	ABS WATT PER SO CM	The second s

TO CONVERT A VALUE FROM A GIVEN UNIT TO A DESIRED UNIT, MULTIPLY THE GIVEN VALUE BY THE FACTOR OPPOSITE THE GIVEN UNITS AND BENEATH THE DESIRED UNIT. NOTE THAT E-XX MEANS 10 TO THE -XX POMER.

ATMOSPHERIC DISPERSION ESTIMATES

* U. S. GOVERNMENT DEDITING OFFICE | 1990-305-382/113

CONVERSION FACTORS - POWER PER UNIT AREA (CAL ARE 15 DEG)